

# Deep exclusive $\pi^+$ electroproduction off the proton at CLAS

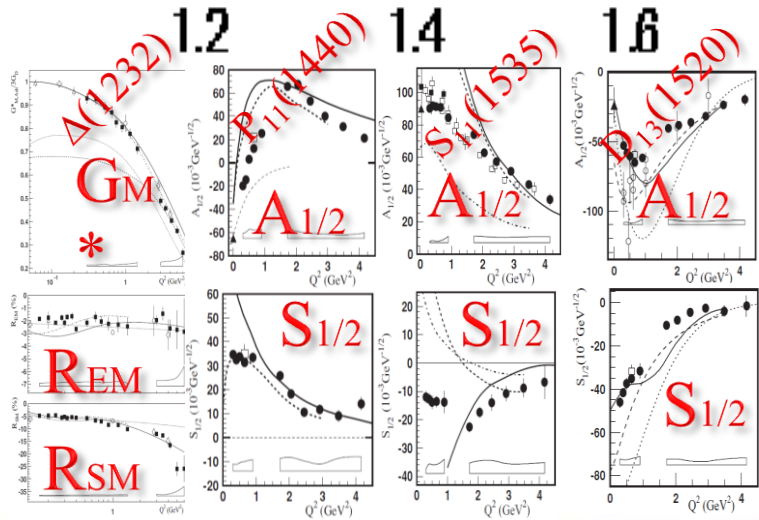
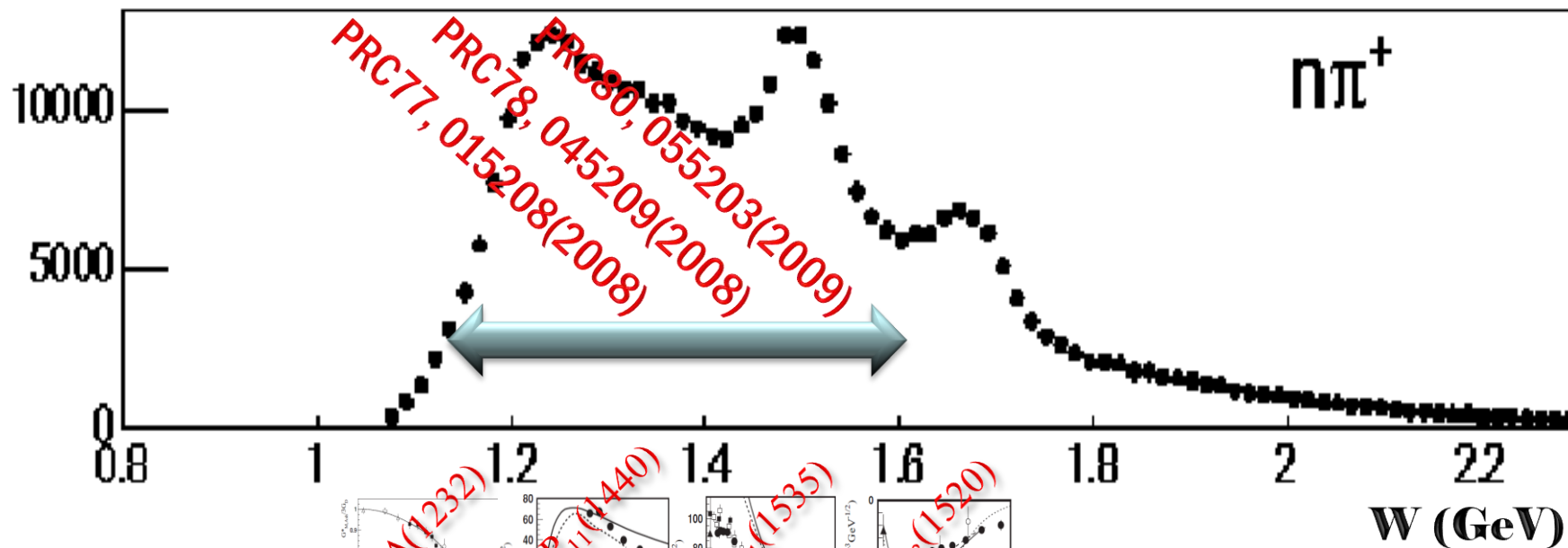
Aug. 13 - 15, 2012  
 $\gamma^*NN^*$  Workshop at USC



# Exclusive single positively charged pion electroproduction off the proton

$$Q^2 < 5.0 \text{ GeV}^2$$

from CLAS

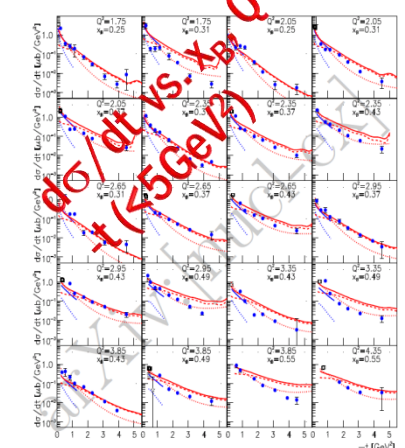
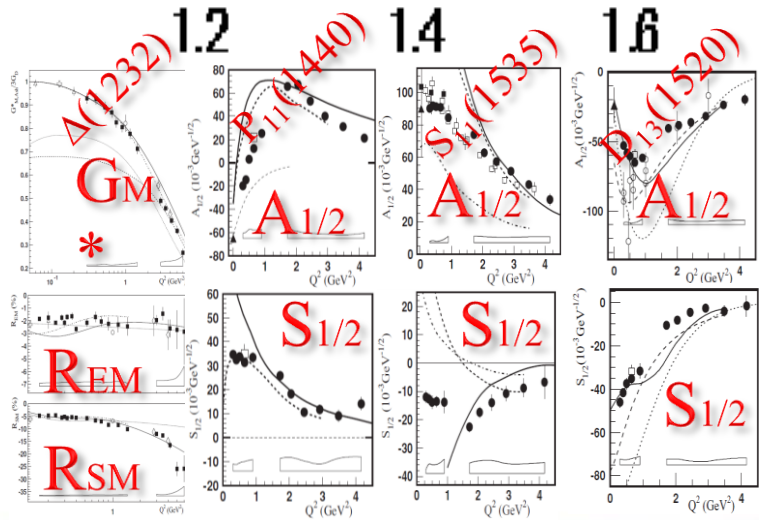
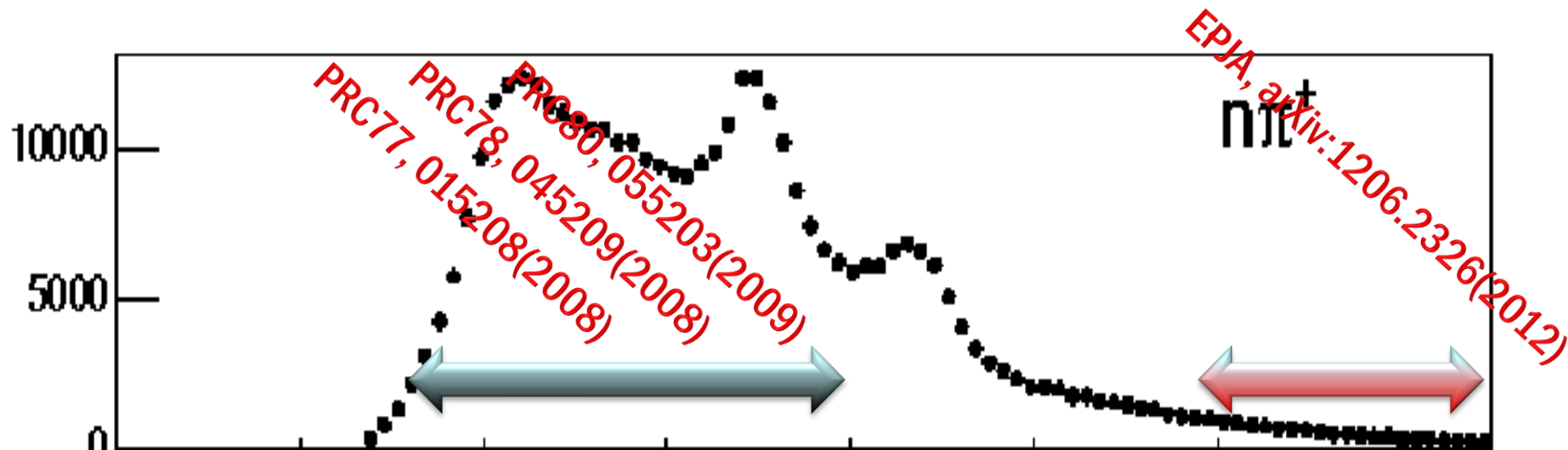




# Exclusive single positively charged pion electroproduction off the proton

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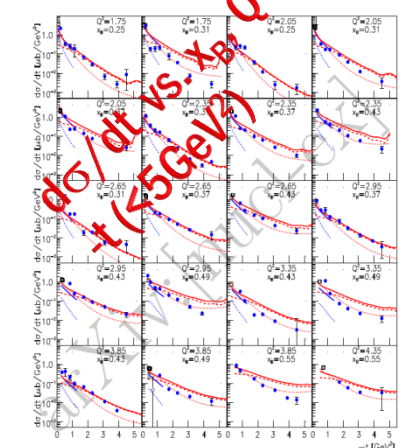
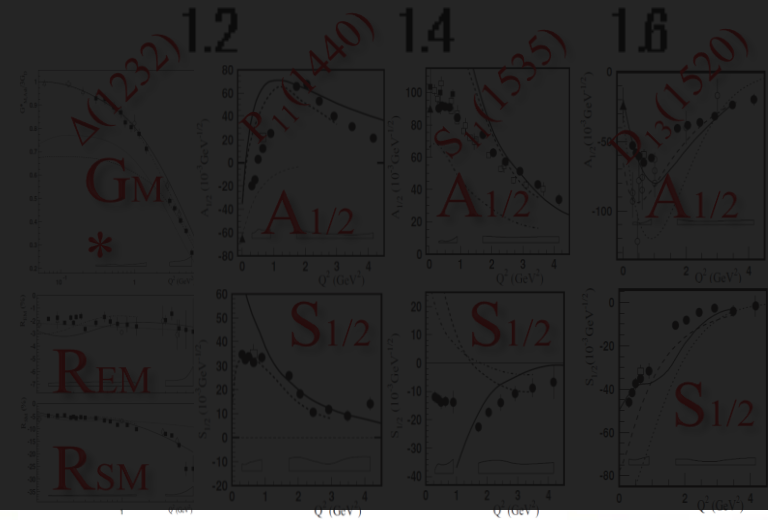




# Exclusive single positively charged pion electroproduction off the proton

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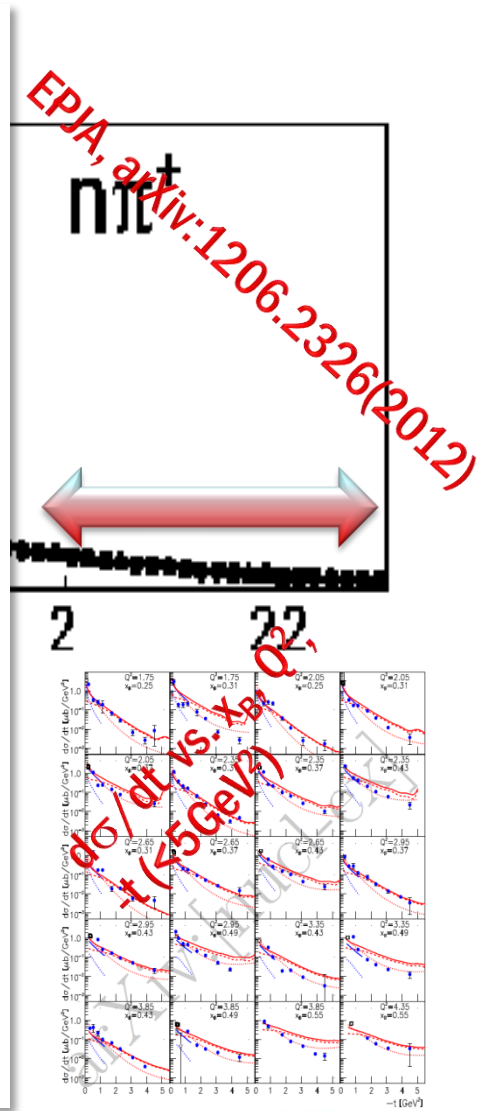


# Exclusive single positively charged pion electroproduction off the proton

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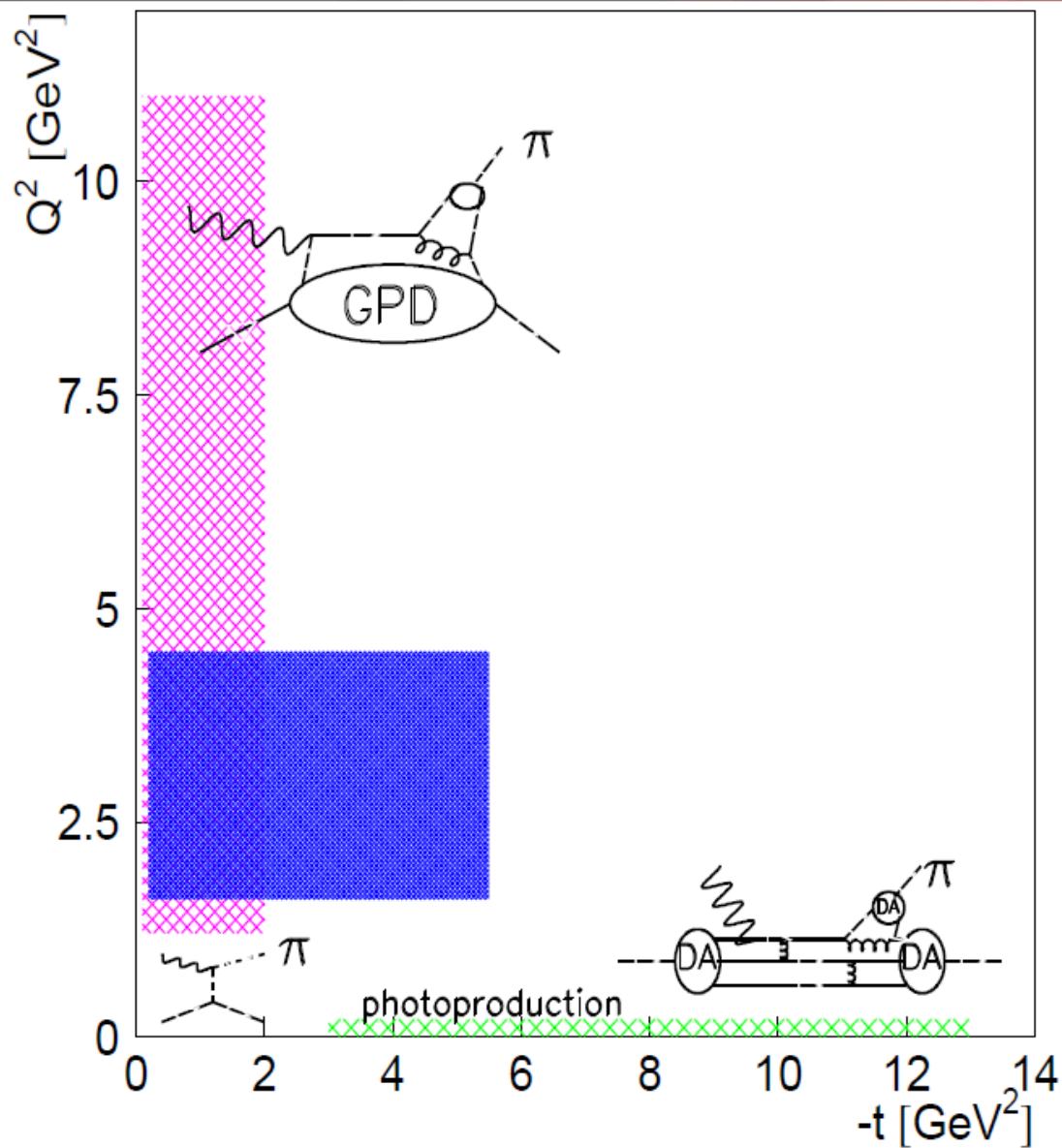
from CLAS

- (1) Transition region
- (2) Scaling ( $s$ -,  $Q^2$ ,...)
- (3) Generalized Parton Distribution
- (4) Transition Distribution Amplitude
- (5) ...



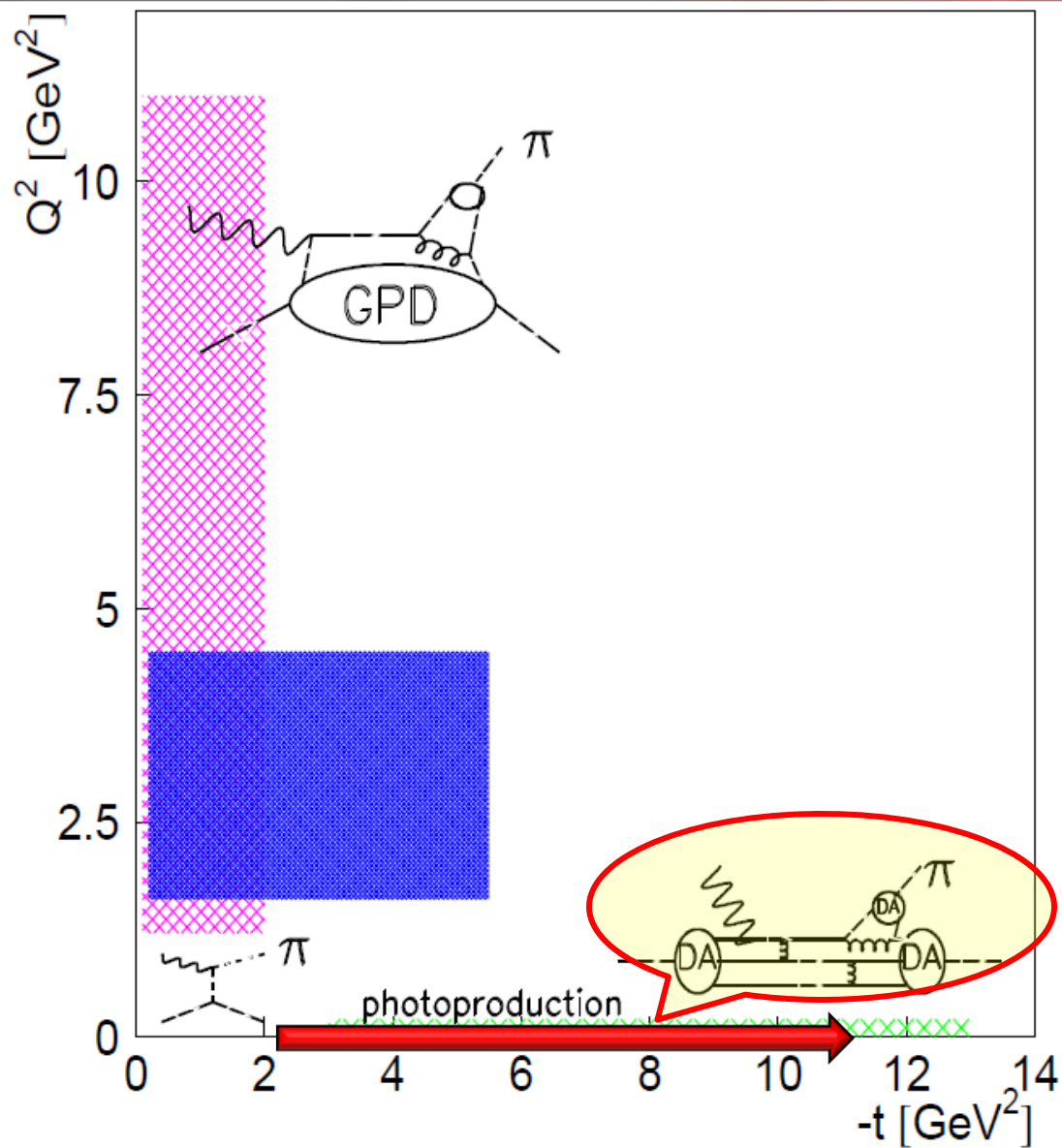


# GPD currently...



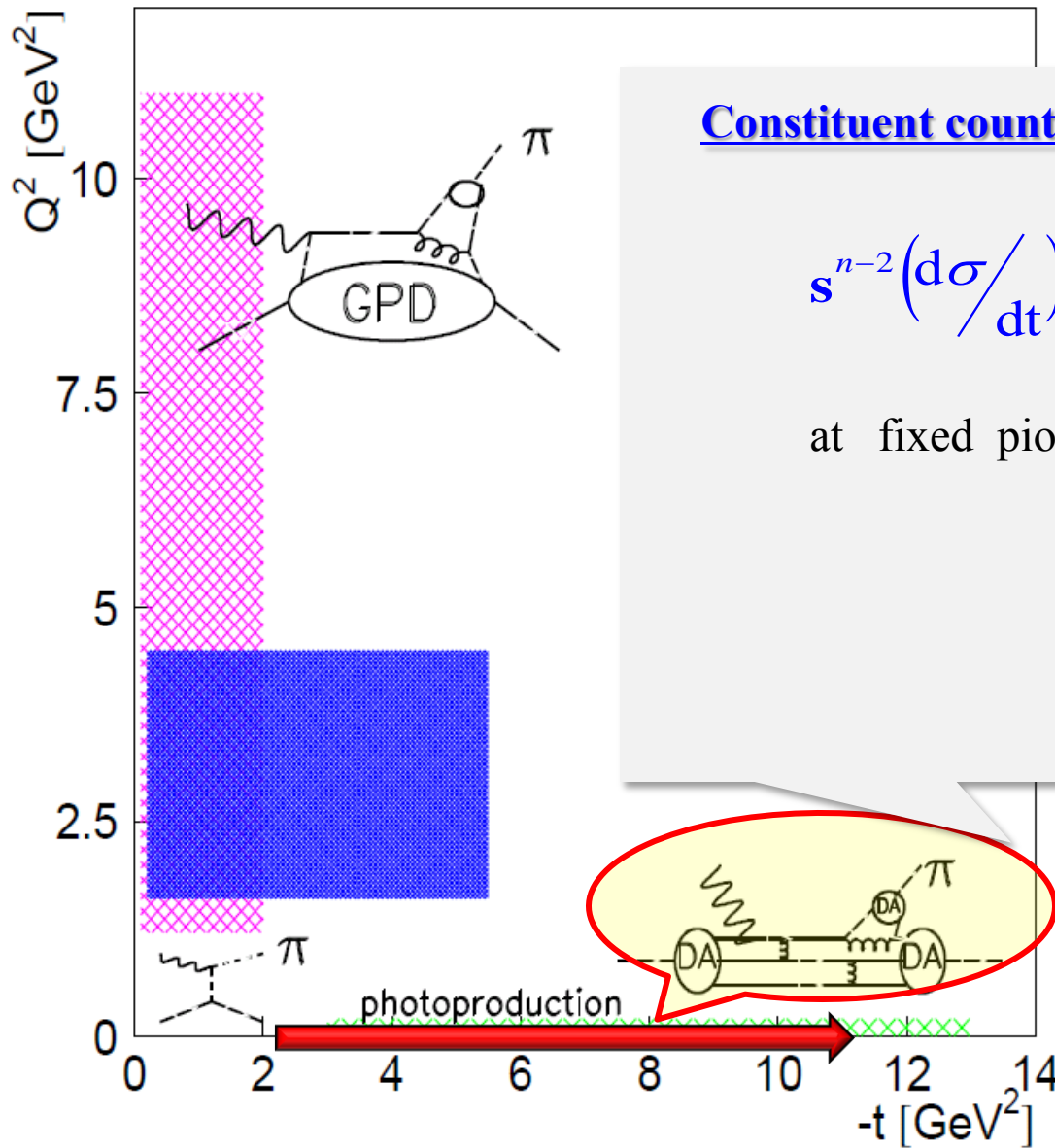


# GPD currently...





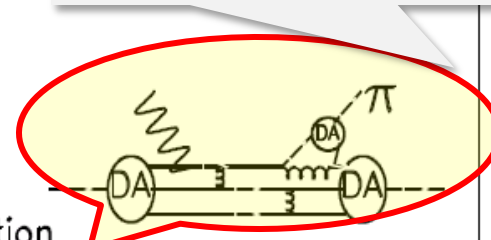
# GPD currently...



## Constituent counting rule (CCR)

$$s^{n-2} \left( \frac{d\sigma}{dt} \right) \propto \text{const.}(s)$$

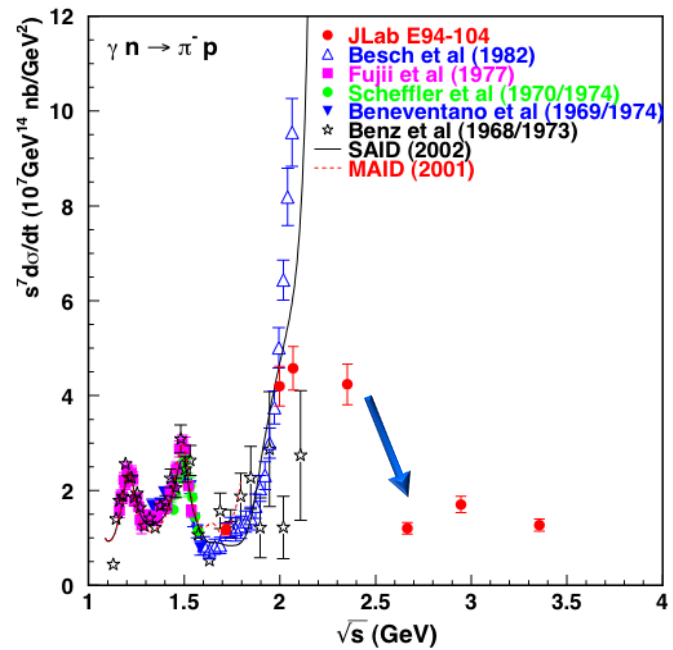
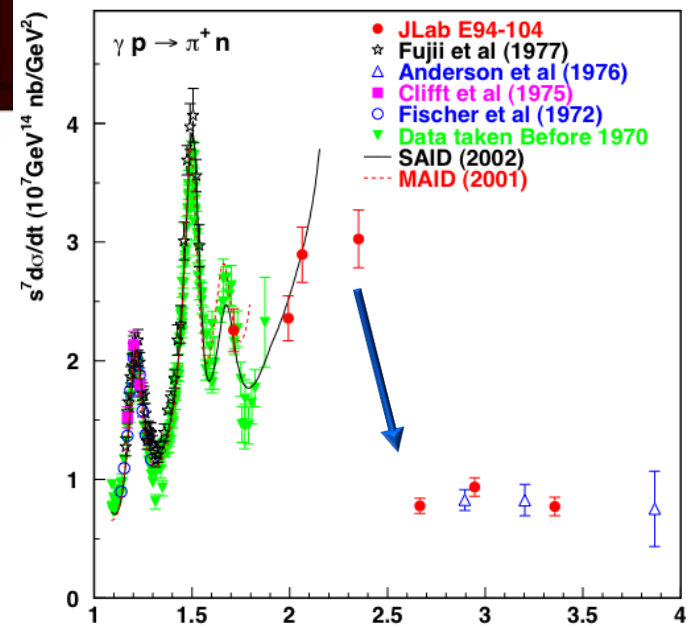
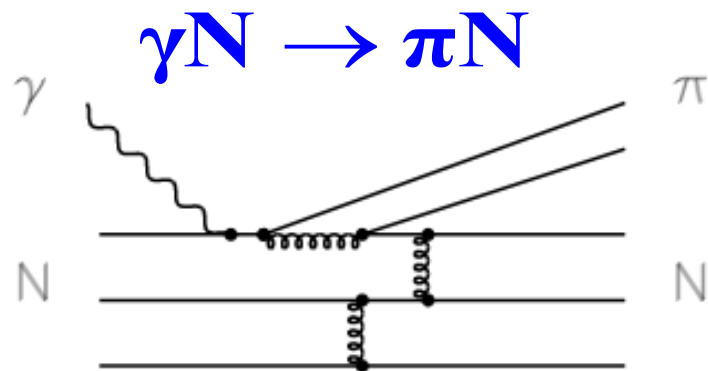
at fixed pion angle (cms)







# Transition observed 90 deg ?



$$\frac{d\sigma}{dt} \propto s^{-2} M^2 \propto s^{-7} \begin{cases} M_{\text{hel. conserving}} \propto s^{-5/2} \\ M_{\text{hel. flipping}} \propto s^{-3} \end{cases}$$

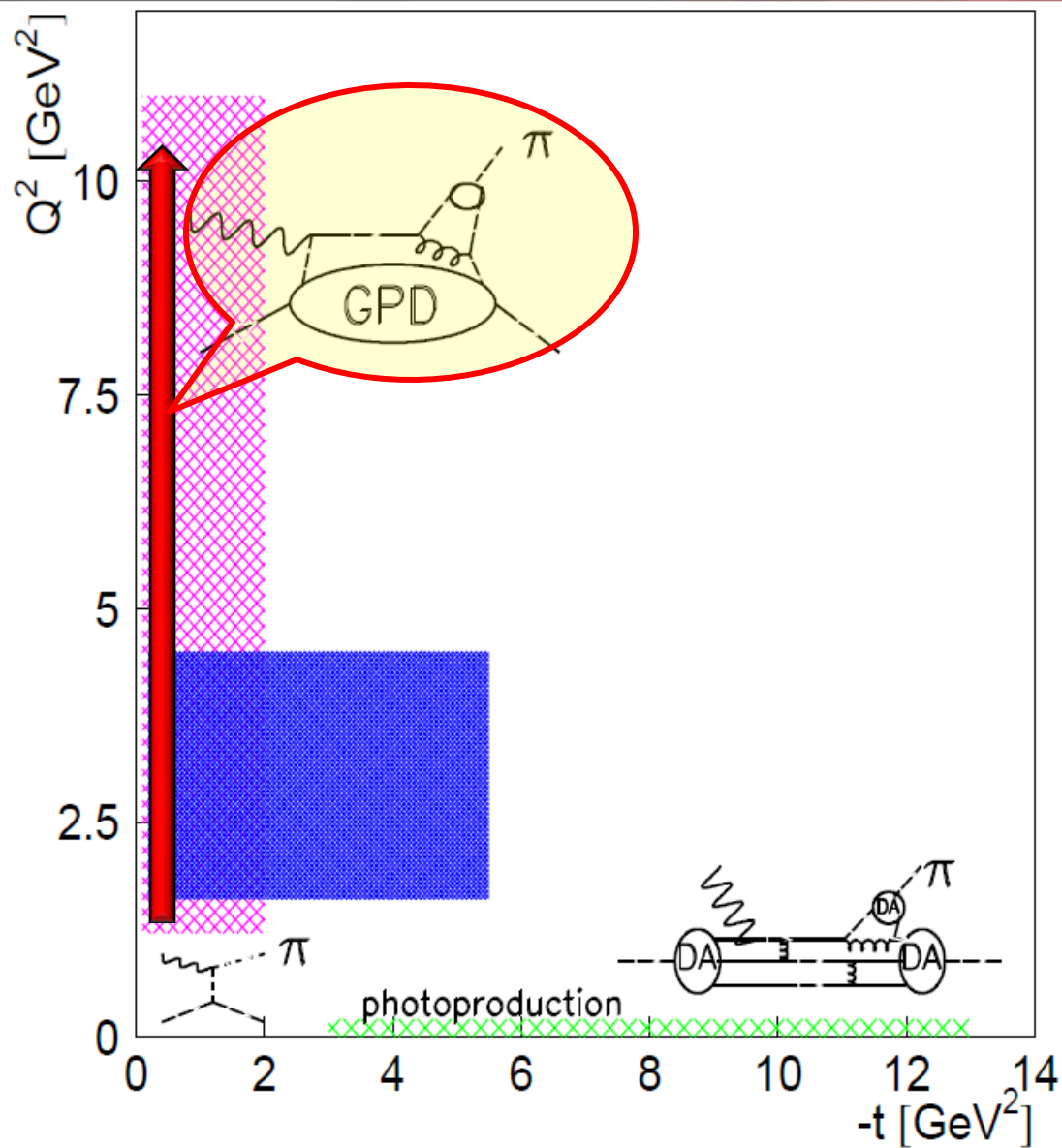
$$\gamma N \rightarrow \pi N ; n-2=7$$

L.Y. Zhu, PRL 91, 022003 (2003)



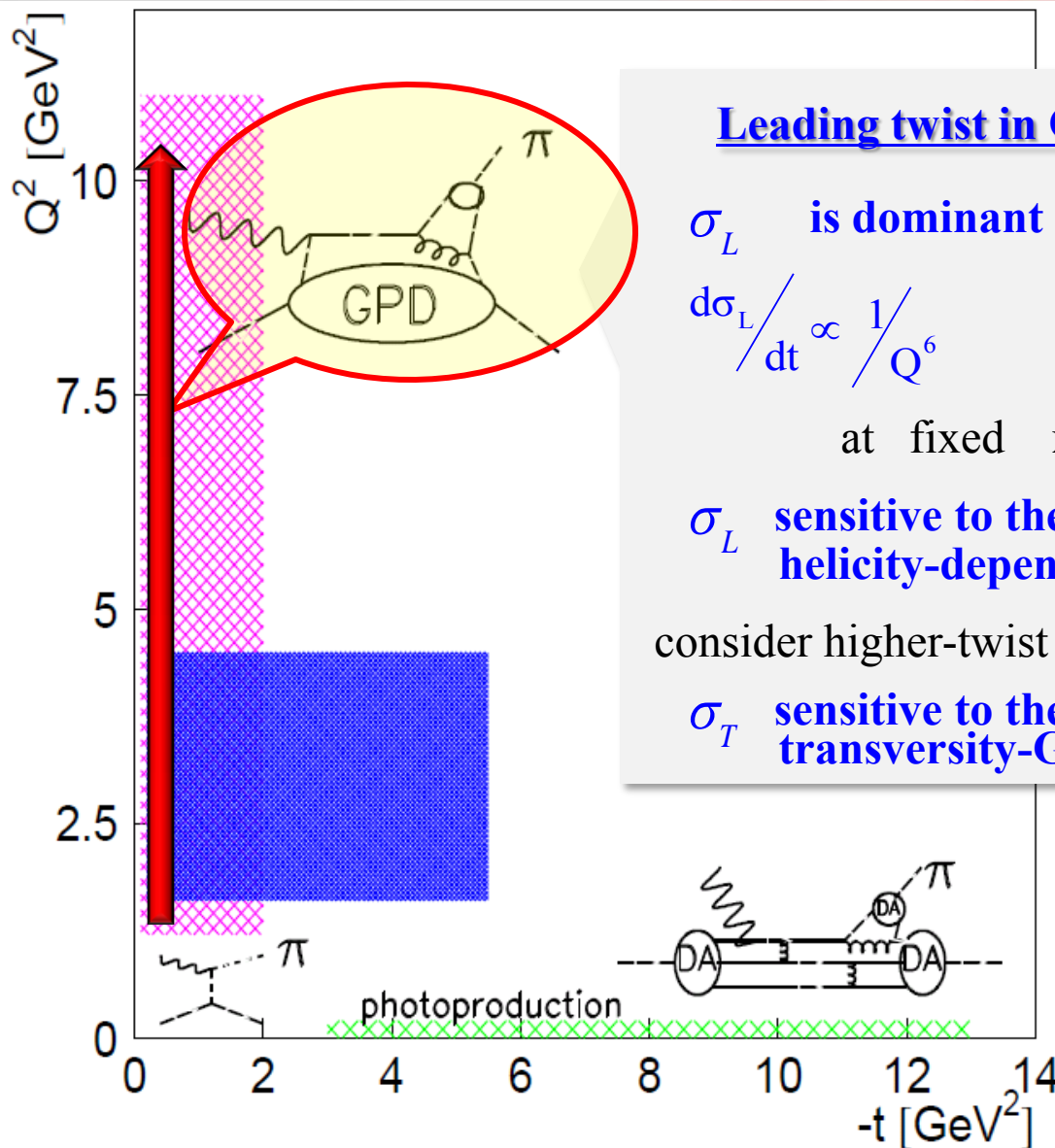


# GPD currently...





# GPD currently...



## Leading twist in QCD for $\pi^+$

$\sigma_L$  is dominant over  $\sigma_T$

$$d\sigma_L/dt \propto 1/Q^6 \quad d\sigma_T/dt \propto 1/Q^8$$

at fixed  $x_B$  and  $|t|$

$\sigma_L$  sensitive to the helicity-dependent GPD  $\tilde{E}$   $\tilde{H}$

consider higher-twist effect

$\sigma_T$  sensitive to the transversity-GPD  $\bar{E}_T$   $\bar{H}_T$

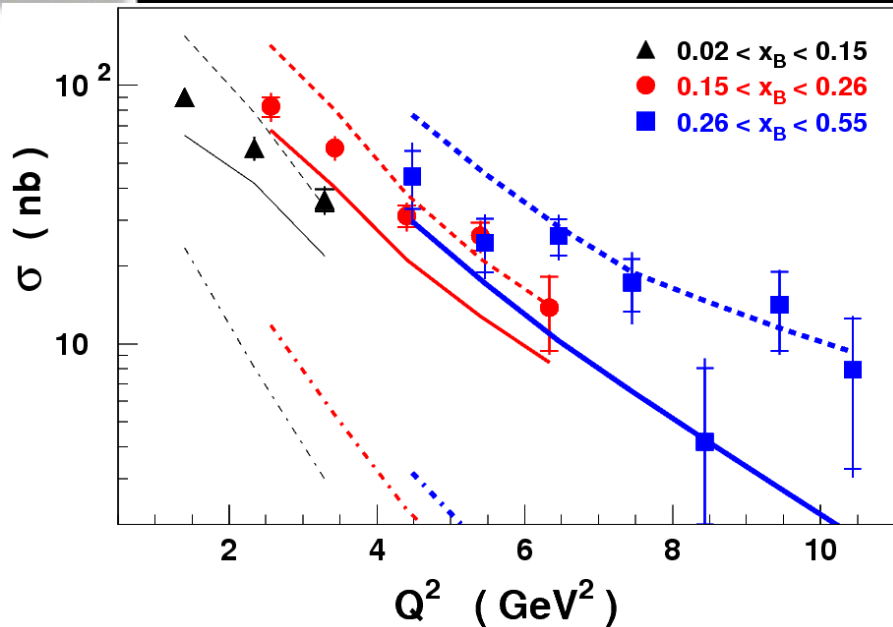


# World Data ... (HERMES)

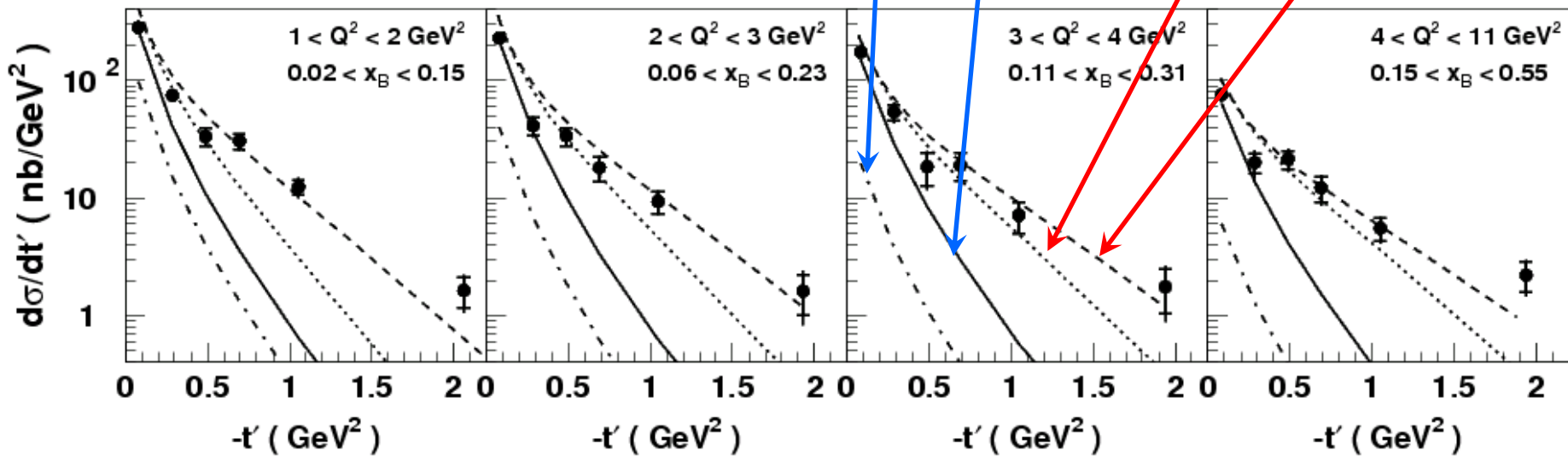
A. Airapetian *et al.*, HERMES collaboration  
Phys.Lett.B 659, 486-492 (2008).  
arXiv:0707.0222v1 (2007).

## GPD Model

Vanderhaeghen, Guichon, Guidal (1999)



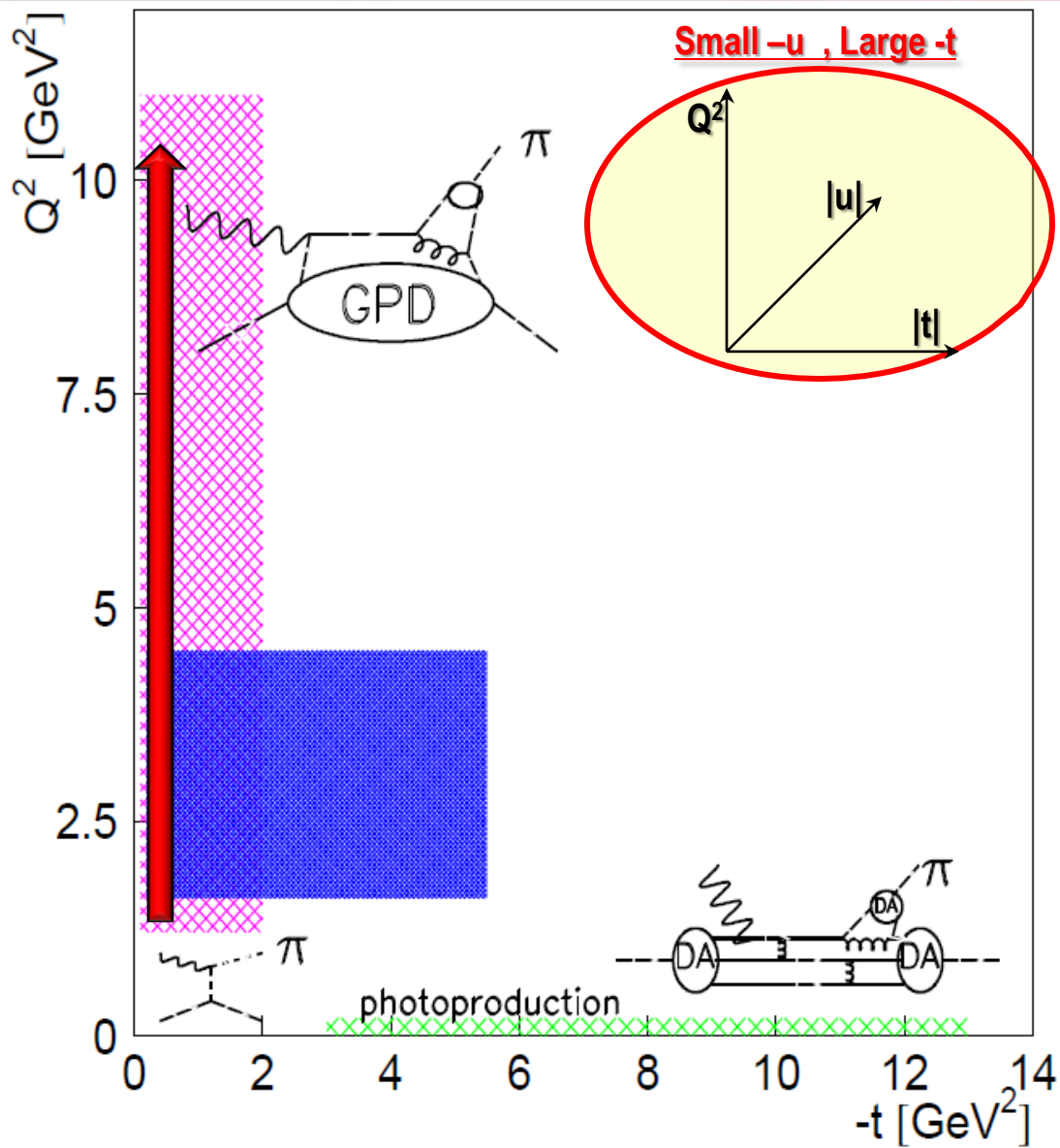
LO calculation  
 Power correction  
 Regge model ( $d\sigma_L/dt$ )  
 Regge model ( $d\sigma/dt$ )





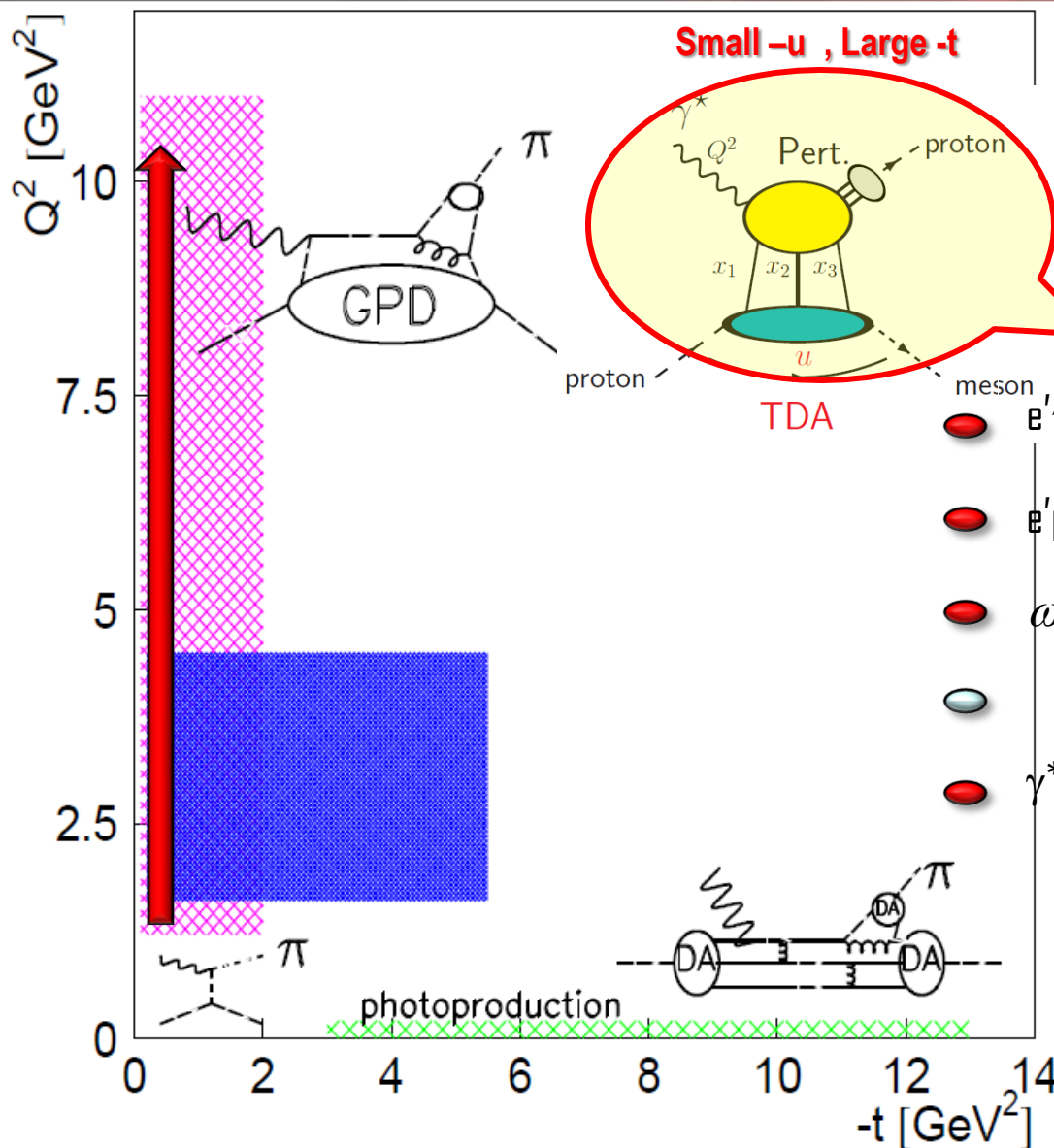


# GPD currently...

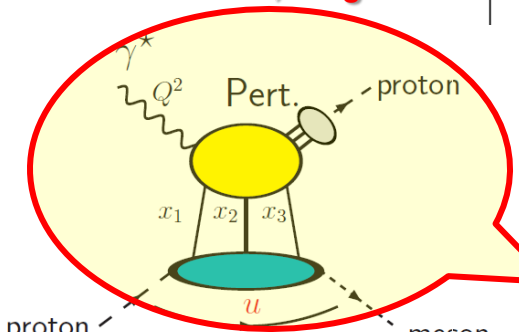




# GPD currently...



Small  $-u$ , Large  $-t$



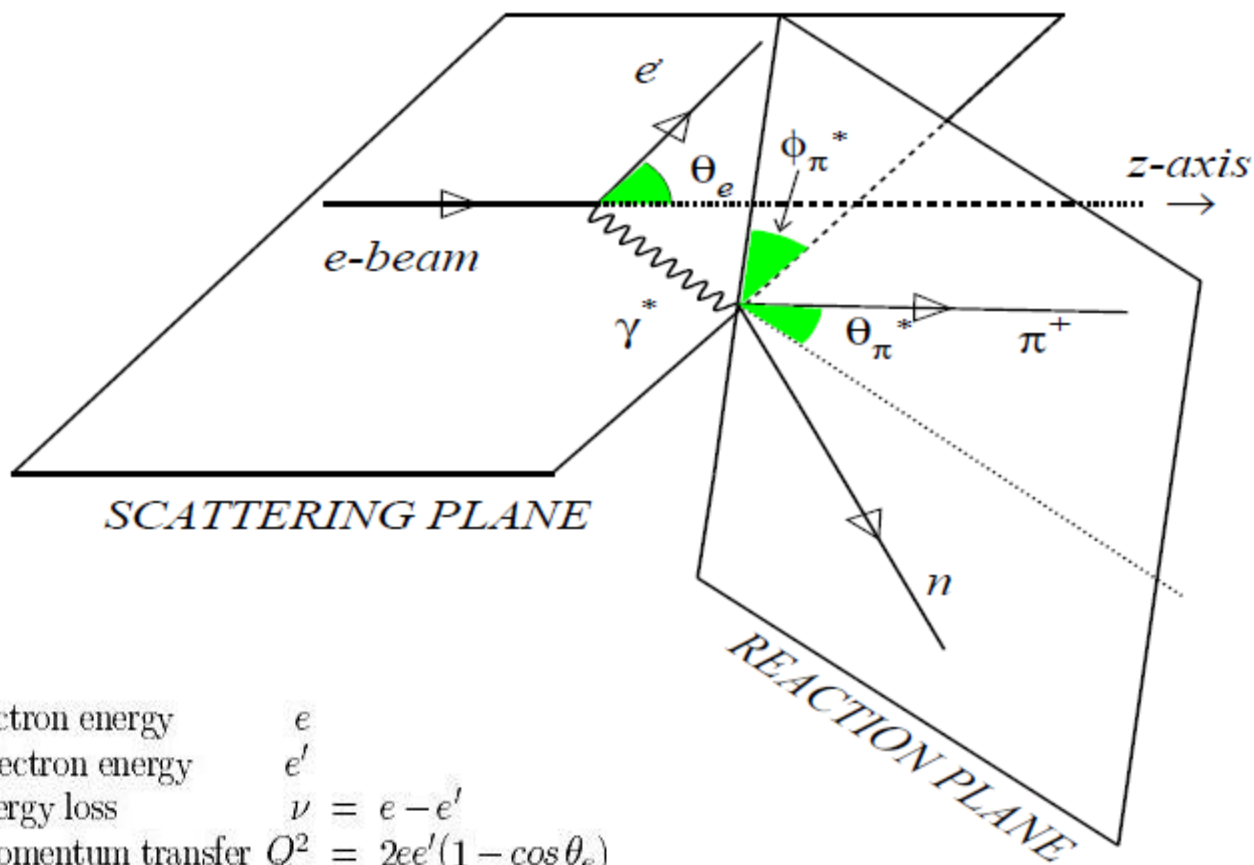
**Baryonic TDA**

- meson  $e' \pi^+ n$   $u \ll, t \gg$  @ CLAS
- $e' p \eta, e' p \pi^0$  @ CLAS
- $\omega$  at  $180^\circ$  @ Hall-C
- JLAB 12GeV
- $\gamma^* p \rightarrow p d / \psi$  @ COMPASS





# Reaction

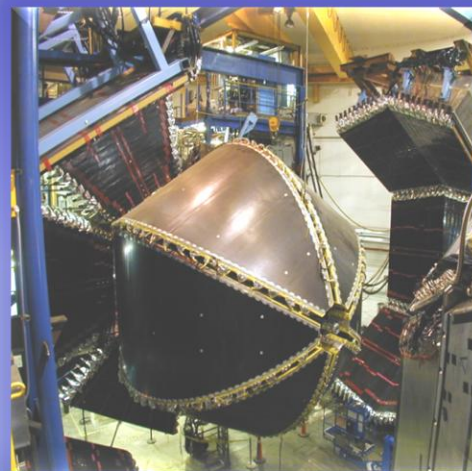


Incident electron energy	$e$
Scattered electron energy	$e'$
Electron energy loss	$\nu = e - e'$
Invariant momentum transfer	$Q^2 = 2ee'(1 - \cos \theta_e)$
Invariant mass of final state	$W = -Q^2 + m_p^2 + 2m_p \nu$
Virtual photon 3-momentum	$ \vec{q}  = (Q^2 + \nu^2)^{1/2}$



# Experimental data /kinematic bin (e1-6 )

- Oct.,2001 ~ Jan., 2002
- $E_0 = 5.754\text{GeV}$  (pol. e), LH2 target
- target position = 4cm upstream
- Length = 5cm,  $\Phi = 6\text{mm}$
- $I_B = 3375\text{A}$
- Trigger =  $E_{Cin} \times E_{Ctot} \times CC$

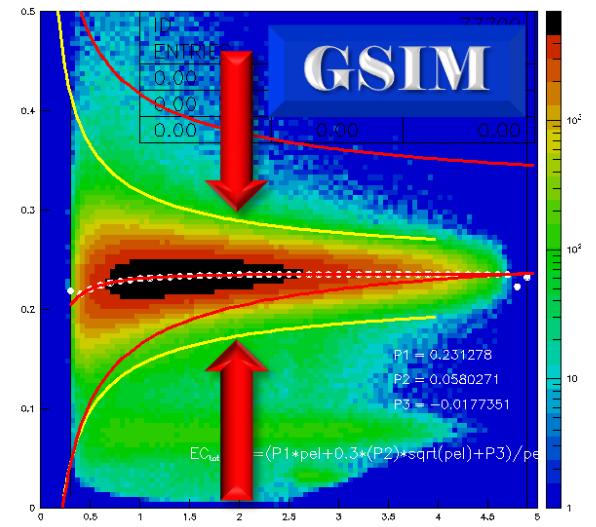
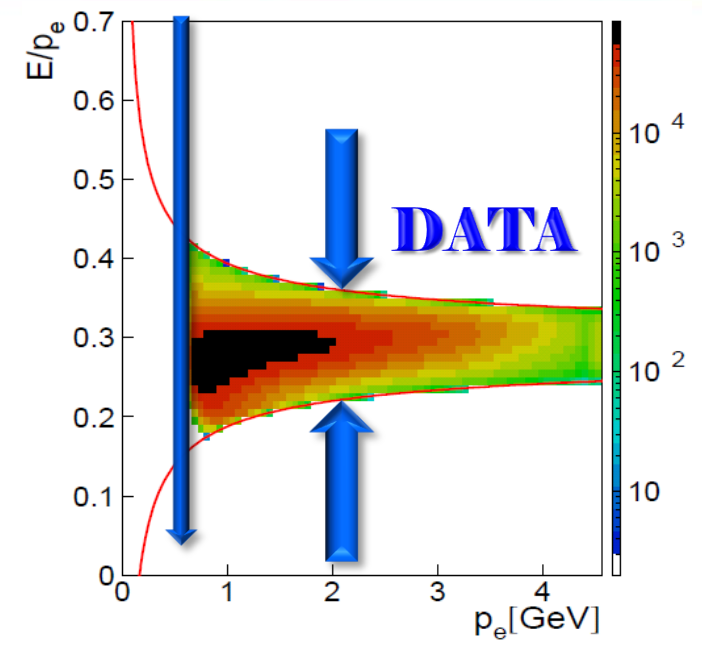
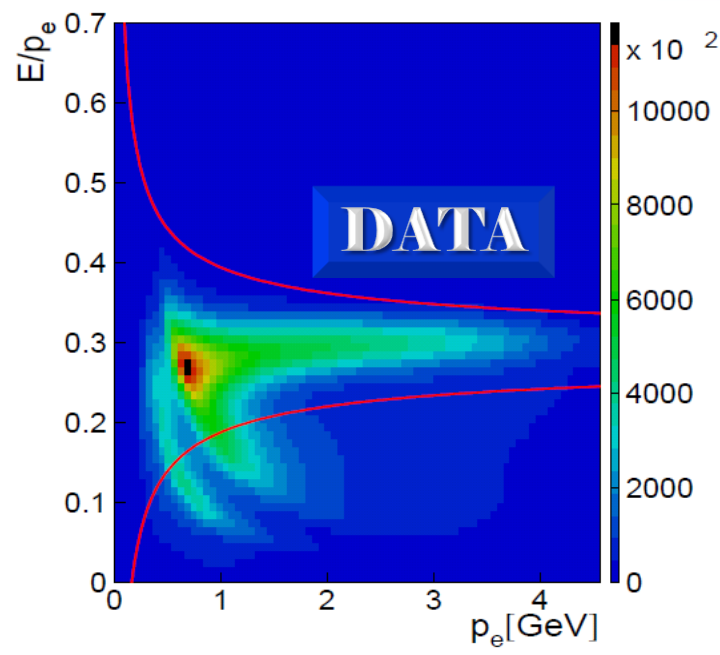


Variable	Number of bins	Range	Bin size
$x_B$	7	0.16 - 0.58	0.06
$Q^2$	5	1.6 - 3.1 $\text{GeV}^2$	0.3 $\text{GeV}^2$
	3	3.1 - 4.5 $\text{GeV}^2$	0.5 $\text{GeV}^2$
$-t$	6	0.1 - 1.9 $\text{GeV}^2$	0.3 $\text{GeV}^2$
	3	1.9 - 4.3 $\text{GeV}^2$	0.8 $\text{GeV}^2$
	1	4.3 - 5.3 $\text{GeV}^2$	1.0 $\text{GeV}^2$

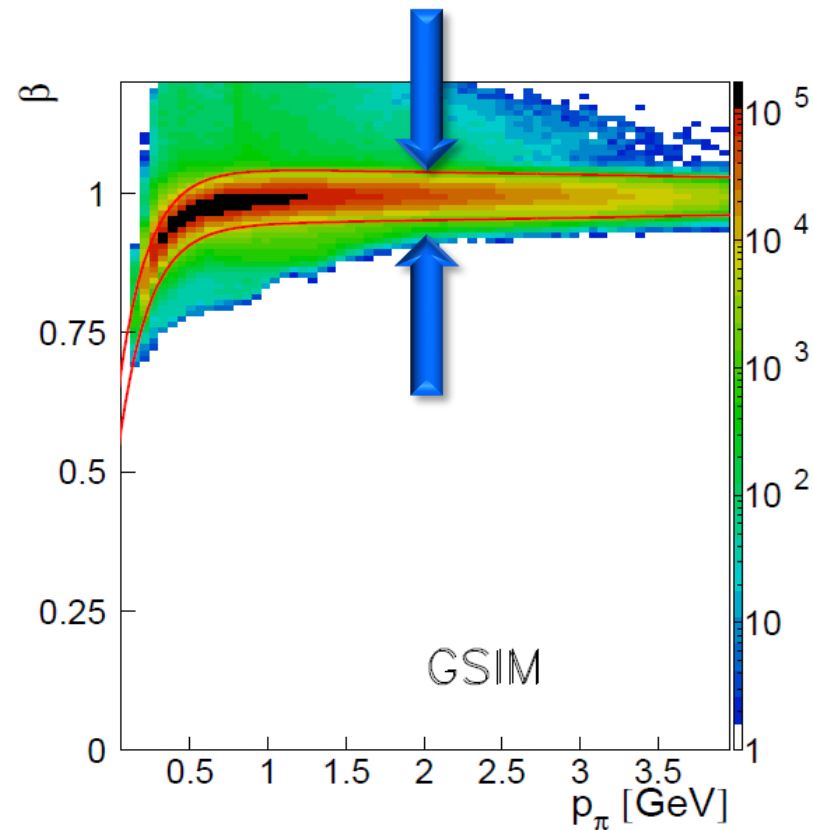
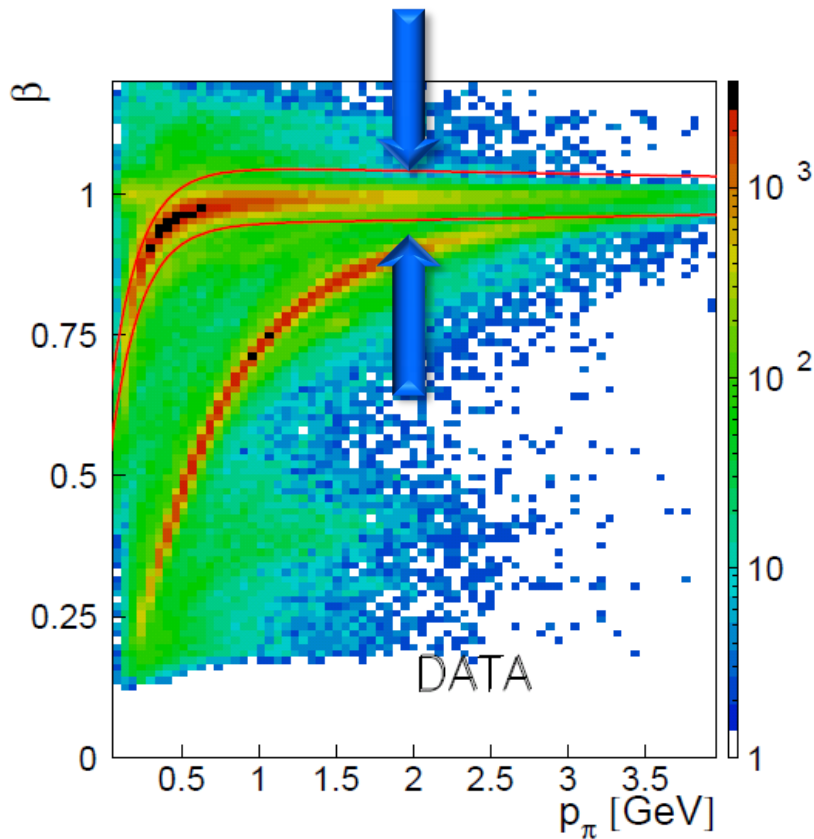


# Analysis - PID electrons

**PID (e)**  
**EC/CC cuts**

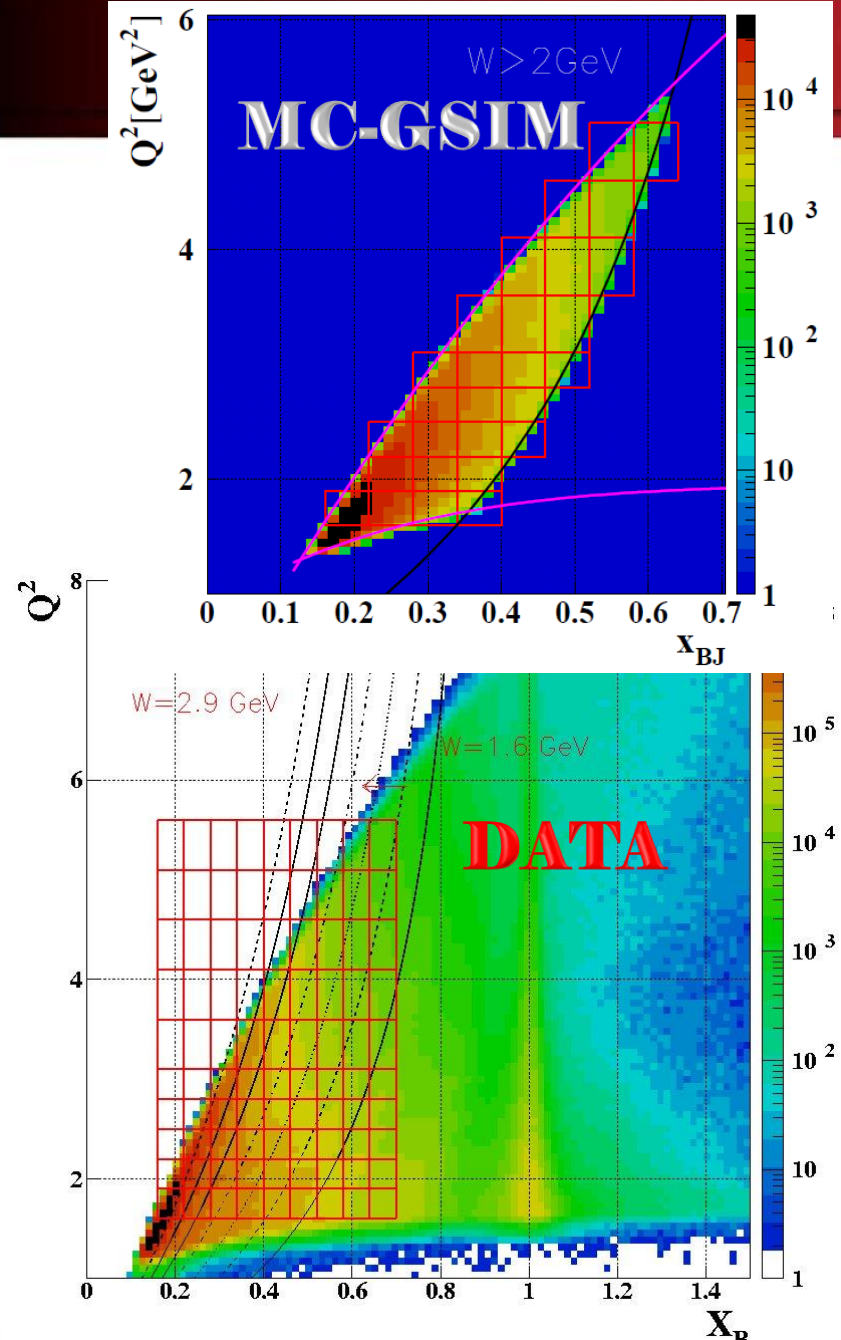
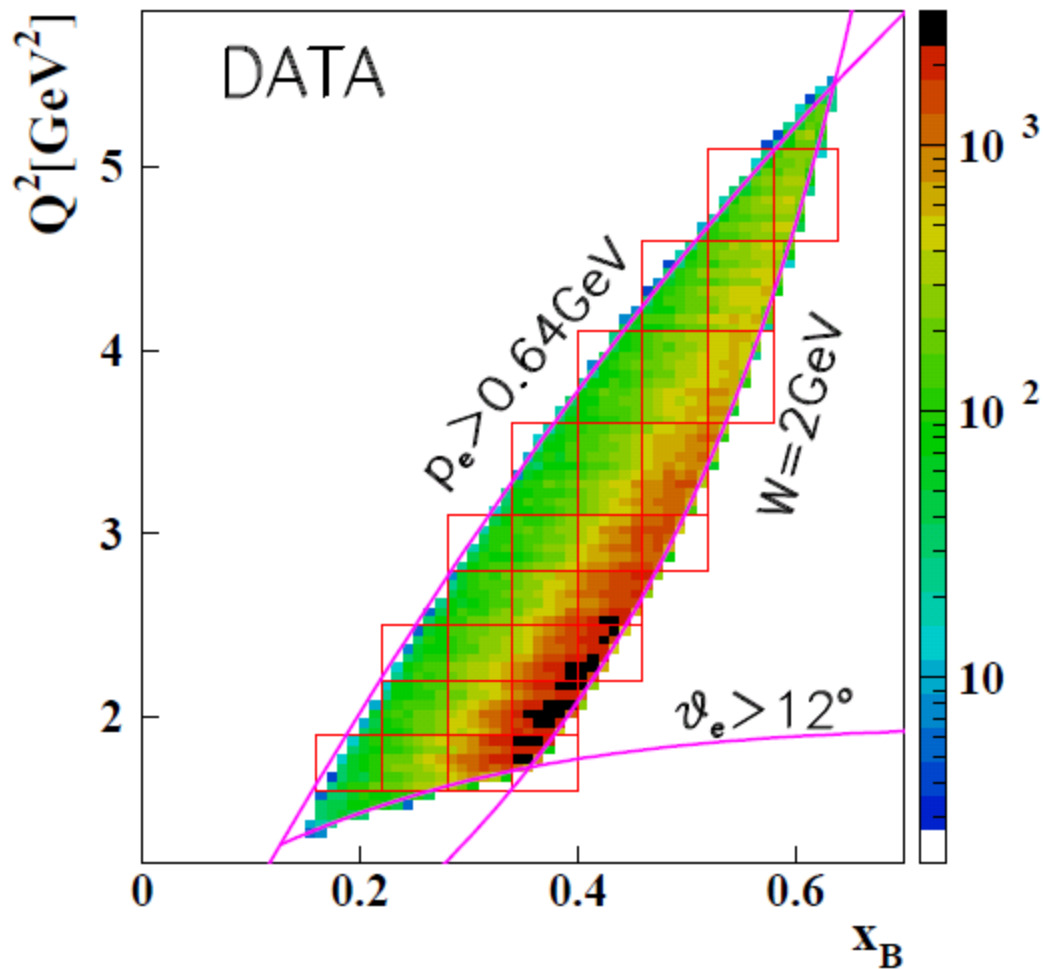


## PID ( $\pi^+$ ) - TOF/DC





# Kinematic coverage

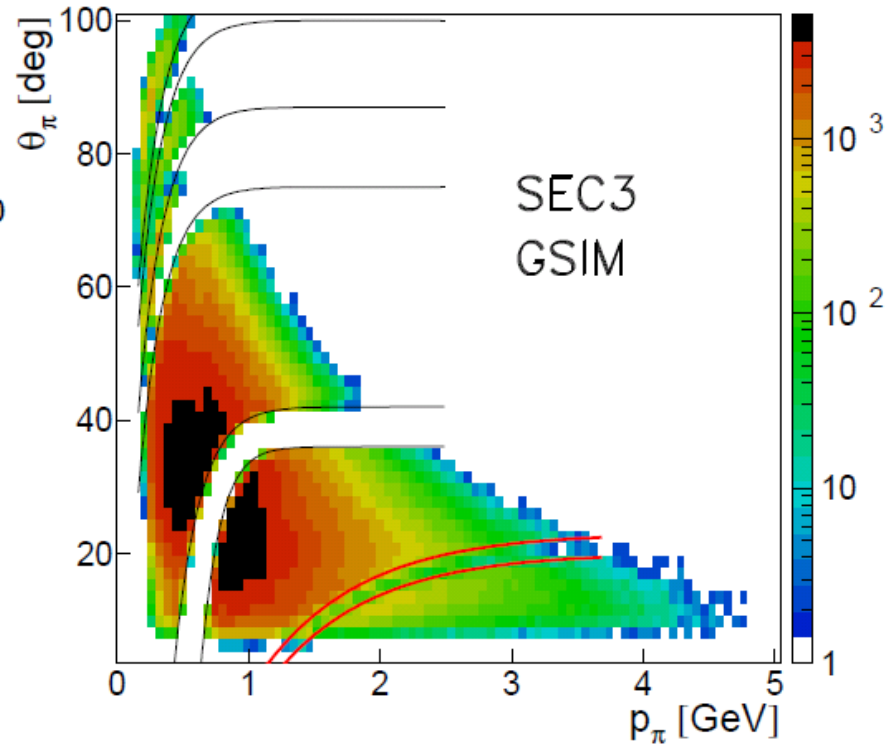
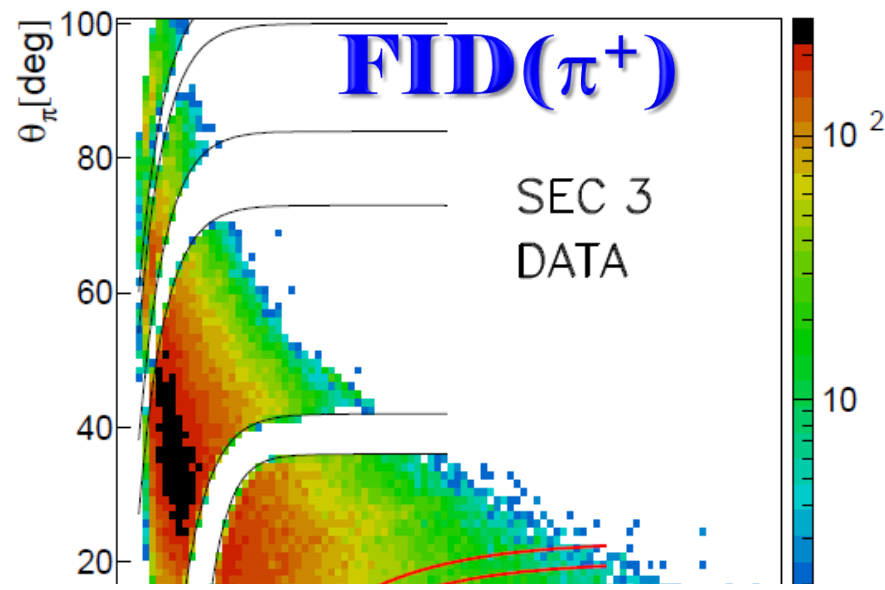
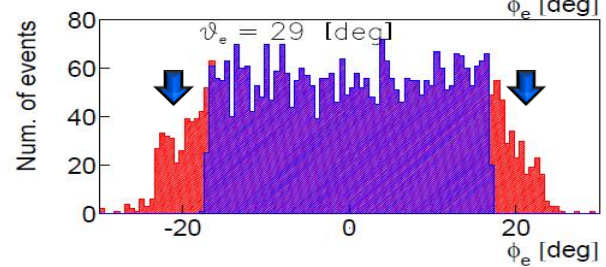
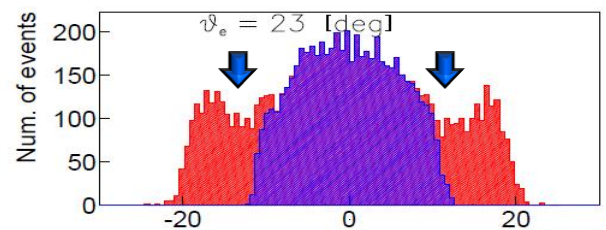
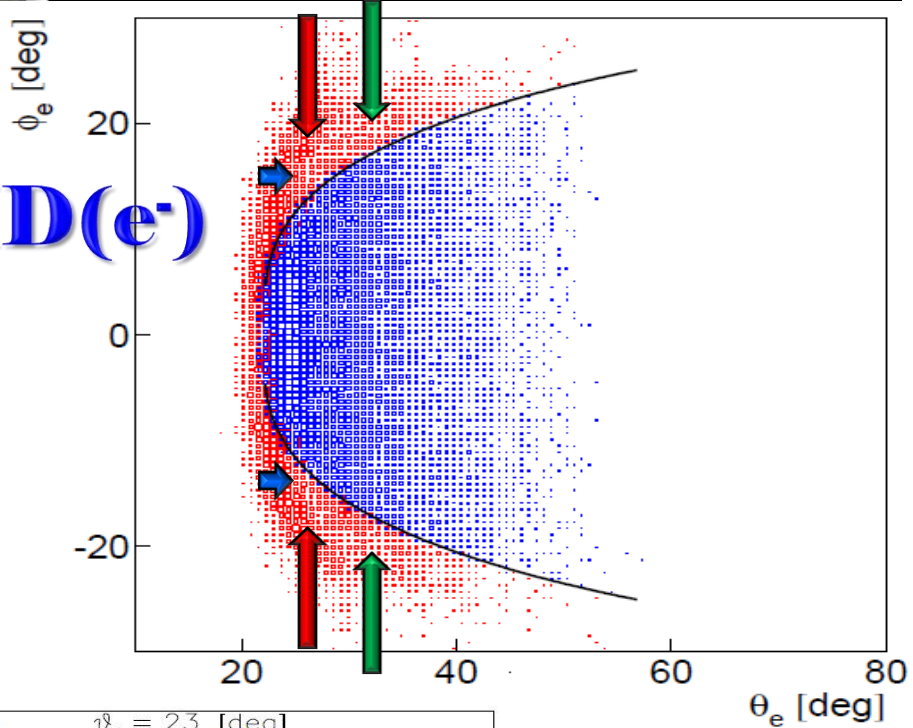






# Analysis - fiducial cuts

## FID( $e^-$ )





## MC – GSIM (acceptances)

- **~850M event generated**
  - **Reconstruction under same cuts as data**
  - **calculate the Acc as function of  $Q^2$ ,  $x_B$ ,  $-t$ , and  $\phi^*$**
1. Exclusive, Semi-inclusive channels have been compared
  2. Missing mass cut applied :  $3.5\sigma$  cut from  $mmx$  resolution ( $\sim 20\text{MeV}$ )
    1. Exclusive : including reaction =  $n\pi^+$
    2. Semi-inclusive : including reactions =  $n\pi^+$ ,  $\Delta^{++}\pi^-$ ,  $\Delta^+\pi^0$ ,  $\Delta^0\pi^+$ ,  $\rho^0p$ ,  $\rho^+n$ ,  $p\pi^+\pi^-$ ,  $n\pi^0\pi^+$ ,  $\omega p$ ,  $p\pi^+\pi^-\pi^0$ ,  $n\pi^+\pi^+\pi^-$ ,  $\phi p$ ,  $p\pi^+\pi^+\pi^-\pi^-$ ,  $p\pi^+\pi^+\pi^-\pi^-\pi^0$ ,  $n\pi^+\pi^+\pi^+\pi^-\pi^-$

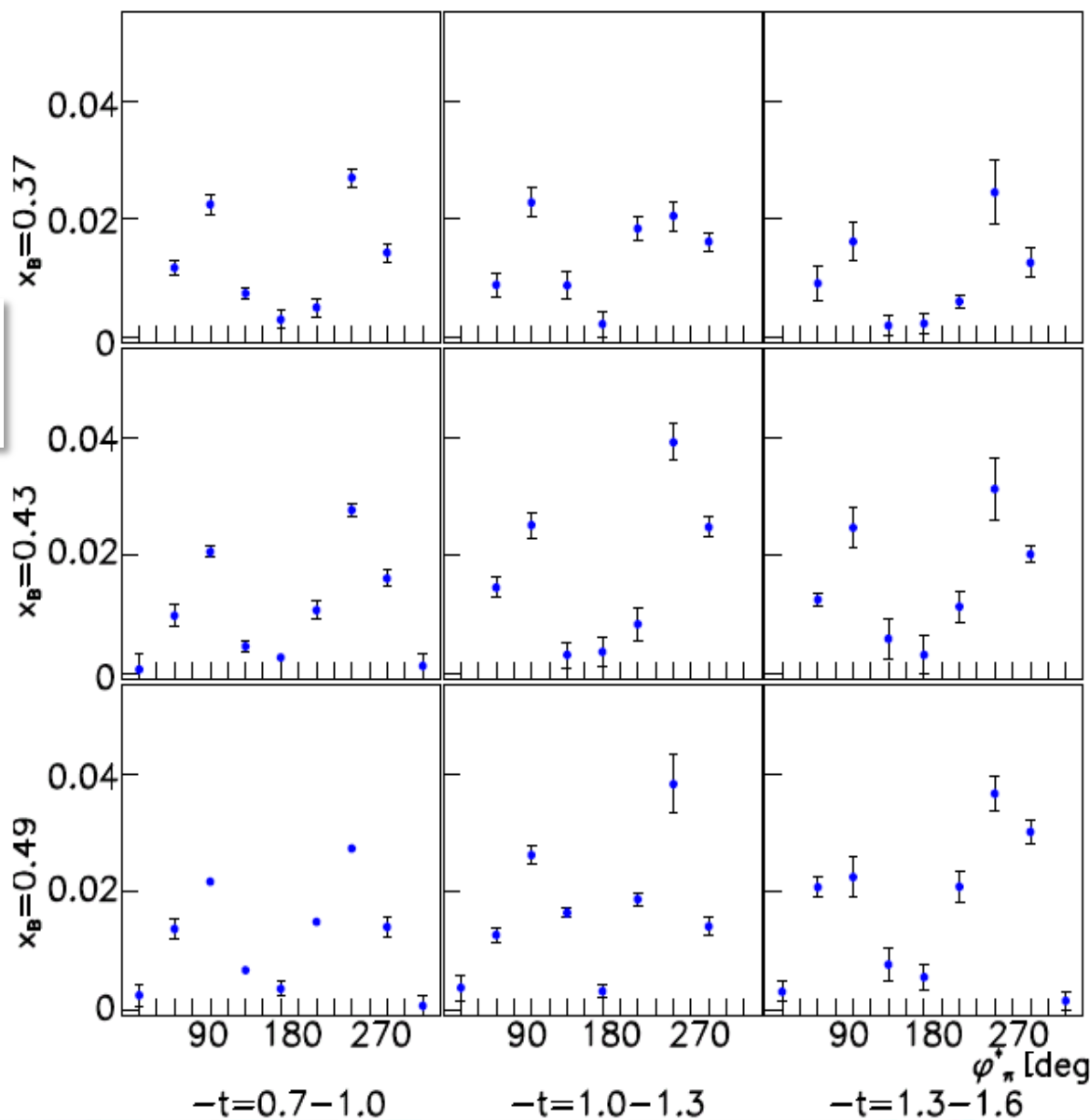


# Acceptance corrections

$$Acc(x_B, Q^2, -t, \phi_\pi^*) = \frac{N^{REC}(x_B, Q^2, -t, \phi_\pi^*)}{N^{GEN}(x_B, Q^2, -t, \phi_\pi^*)}$$

$N^{REC}$  the number of reconstructed particles

$N^{GEN}$  the number of generated particles

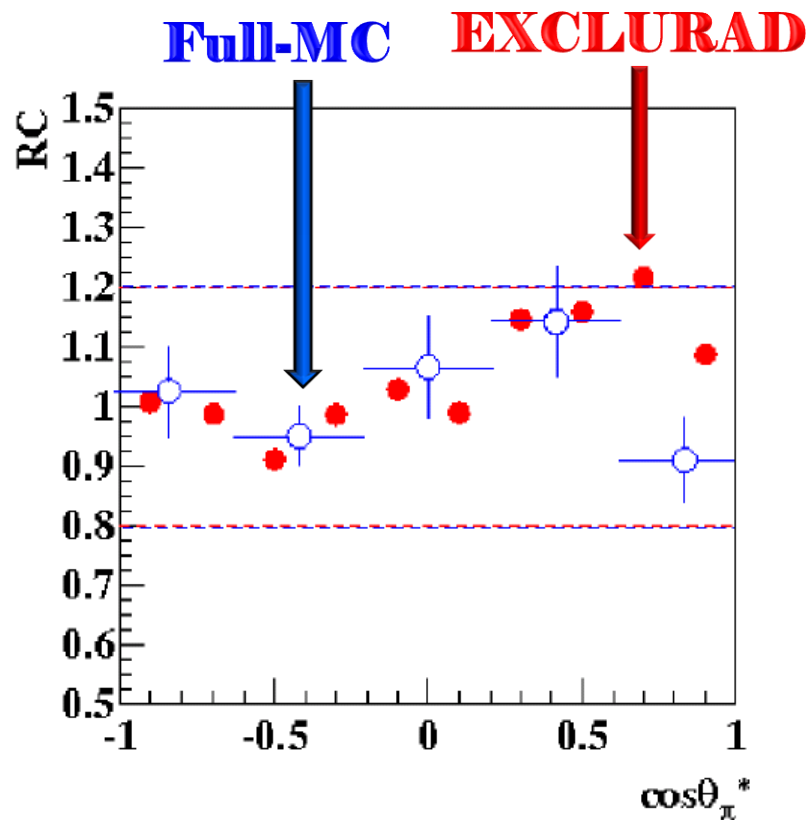
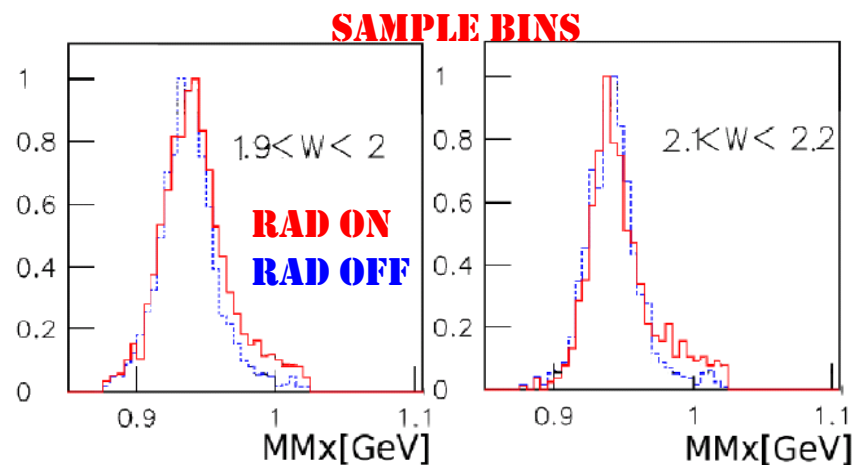




# Radiative correction with full-simulation

## Fact(s)

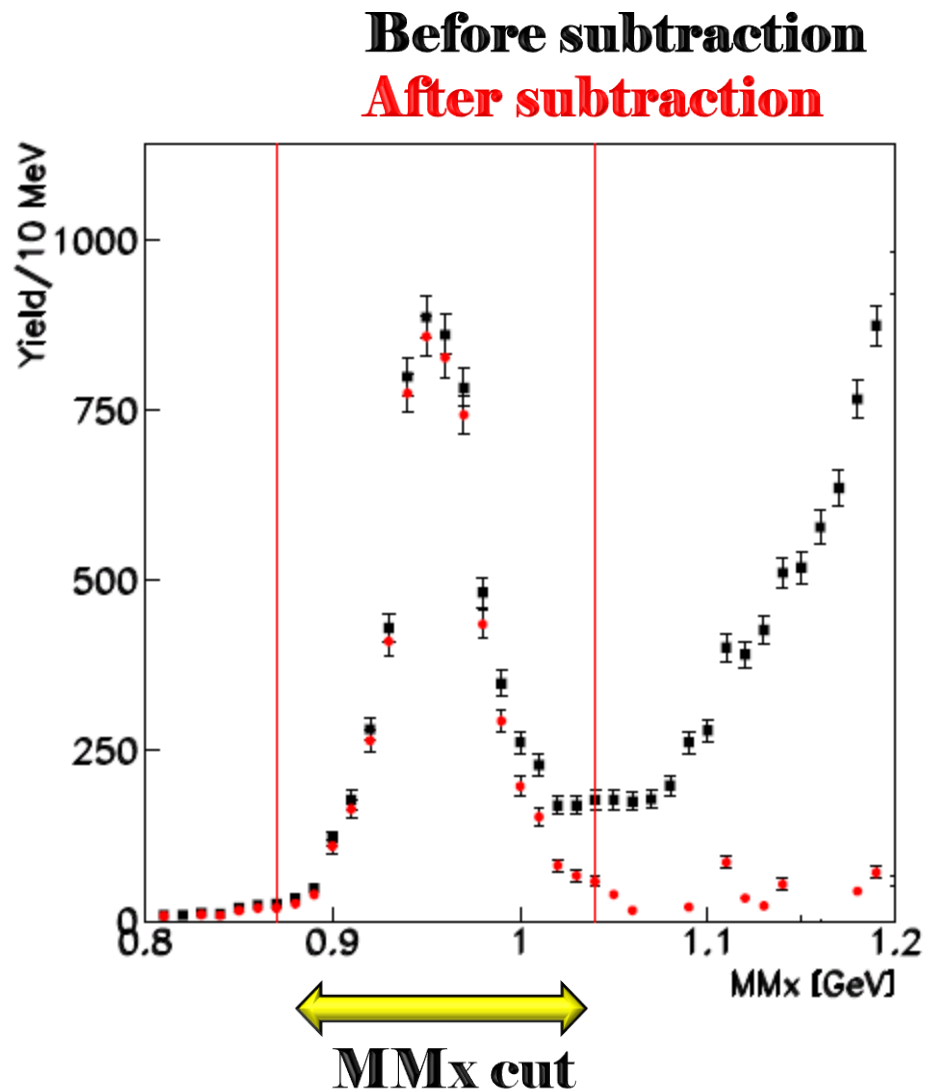
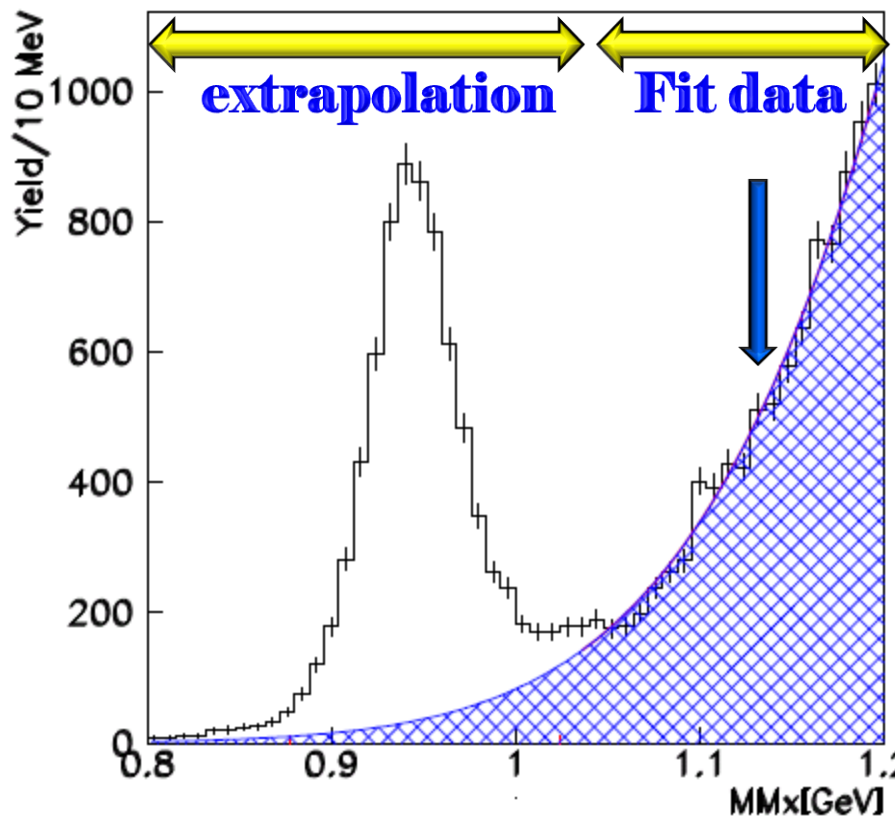
- (1) No model support to EXCLURAD for radiative correction ( $W < 2\text{GeV}$ )
- (2) GENEV full-simulation shows a reasonable good agreement with EXCLURAD's result in the valid kinematic region for both



**$W \sim 1.75 \text{ GeV}$**   
 **$Q^2 \sim 3 \text{ GeV}^2$**   
 **$\phi^* = 80\text{-}120 \text{ deg}$**



# Background subtraction





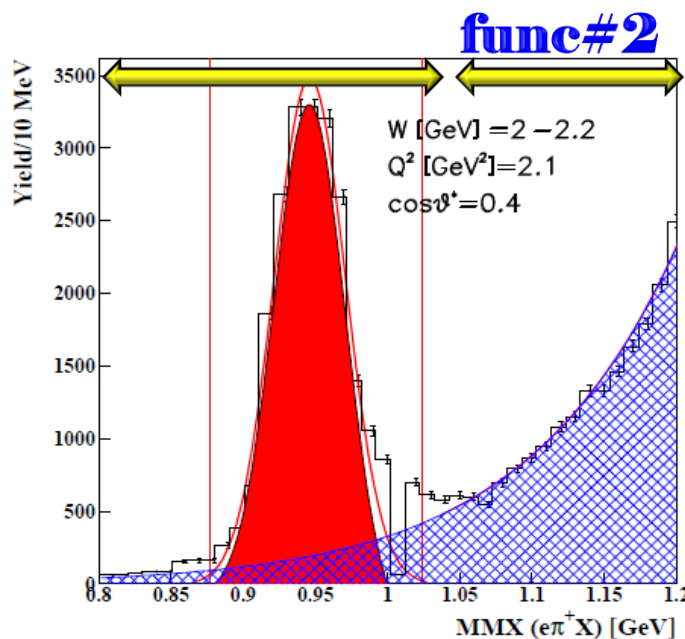
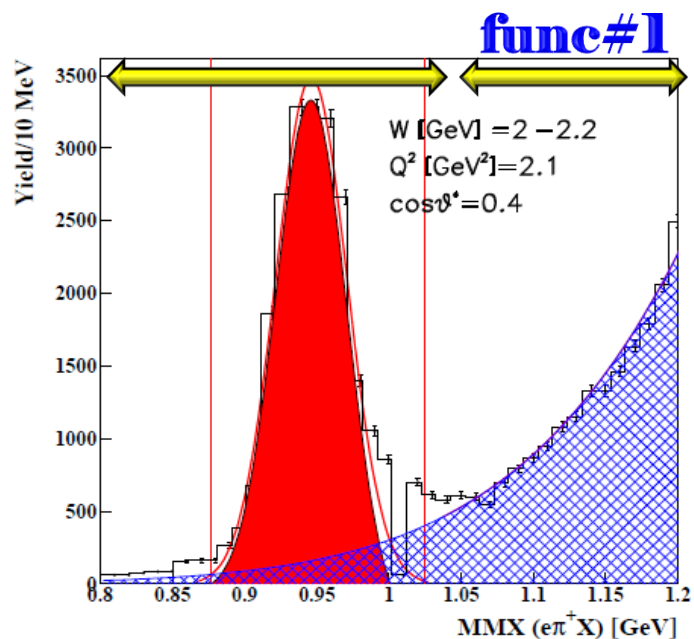
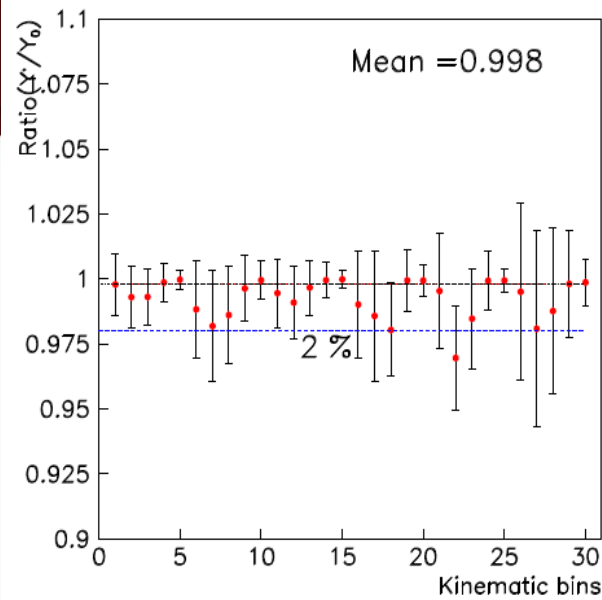


# Background subtraction

$$ratio = \frac{Y'(n\pi^+)}{Y_0(n\pi^+)}$$

$Y_0$  is the yield with nominal BG subtraction,

$Y'$  is the yield with subtraction of the BG and the left tail of missing mass neutron



**Same fit range**  
**Different functions**

**func#1 : G + pol3**  
**func#2 : E + pol2**

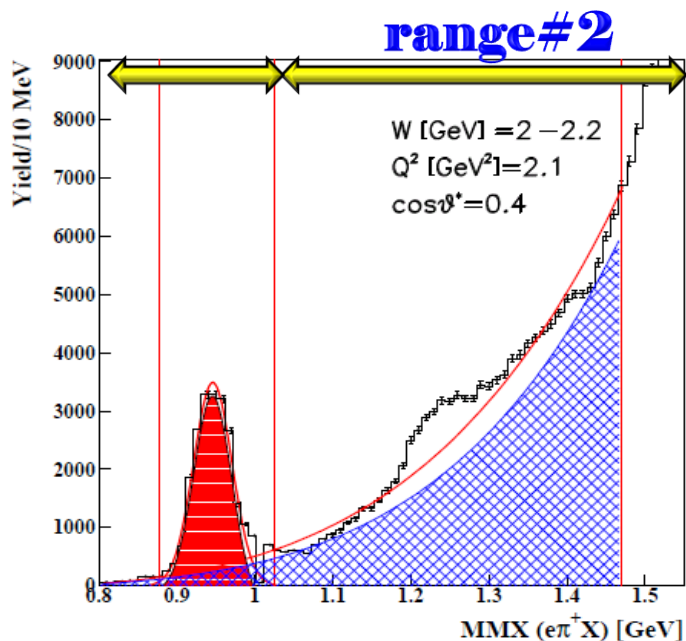
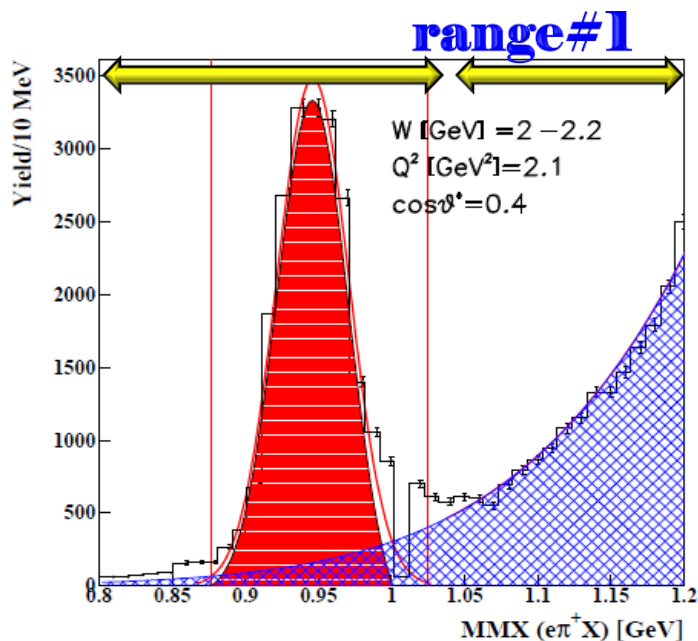
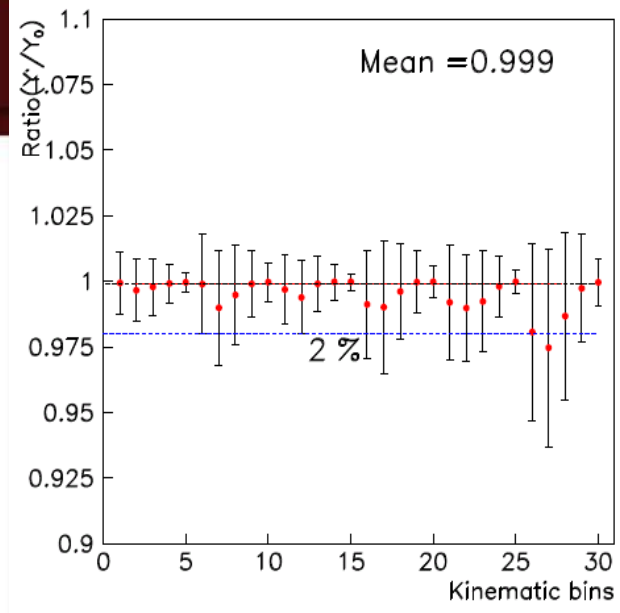


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$Y_0$  is the yield with nominal BG subtraction,

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**Same function**  
**Different fit**  
**ranges**

**range#1 :**  
**0.8 - 1.2 GeV**

**range#2 :**  
**0.75 - 1.45 GeV**

**\*\* away from radiative tail**

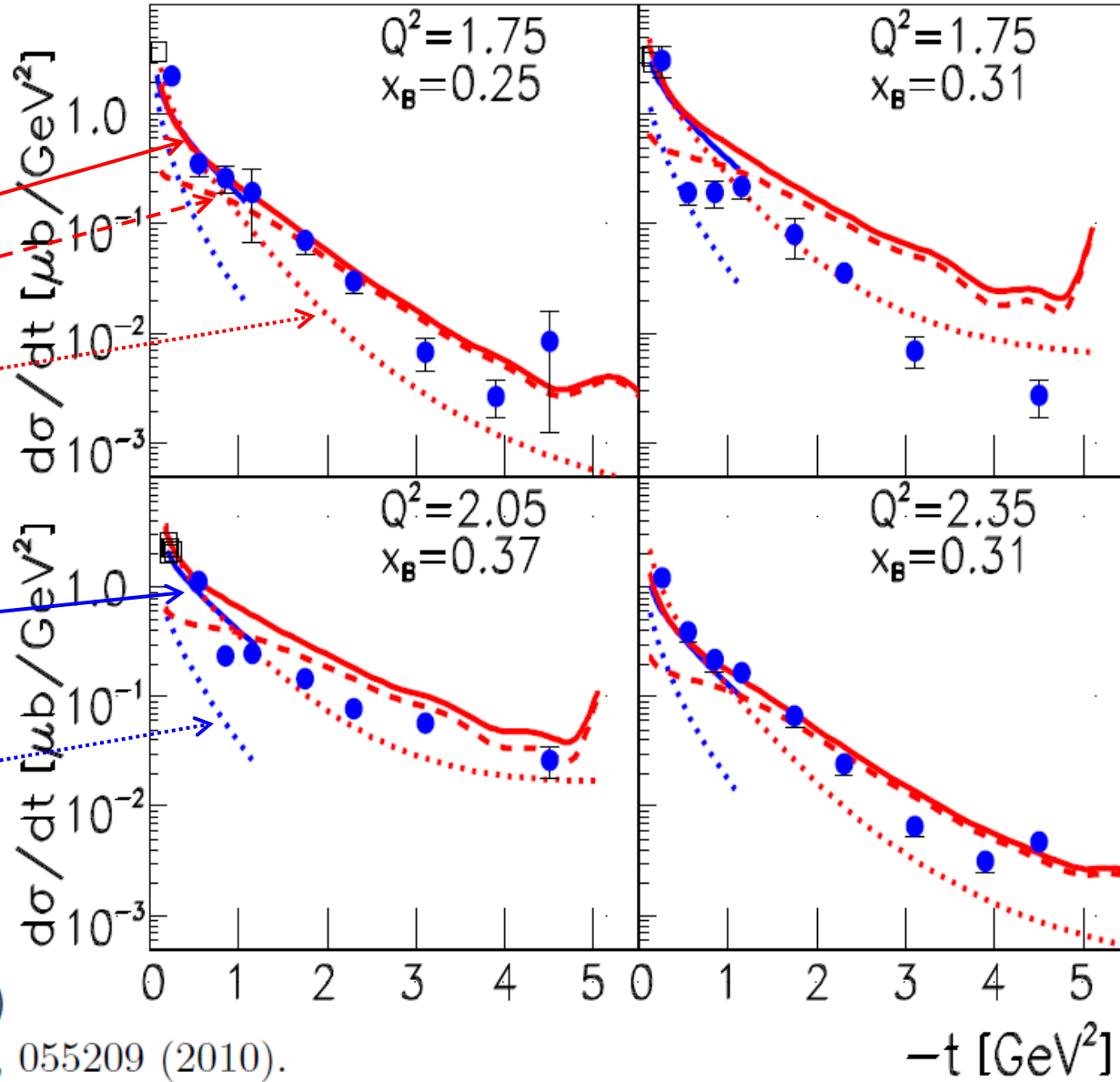


# Cross-sections vs. -t

$$\frac{d\sigma}{dt} = \frac{1}{\Gamma} \frac{d^3\sigma}{dQ^2 dx_B dt}$$

**Laget**  $d\sigma/dt$   
 $d\sigma_T/dt$   
 $d\sigma_L/dt$

**GK**  $d\sigma/dt$   
 $d\sigma_L/dt$



JLab Hall C

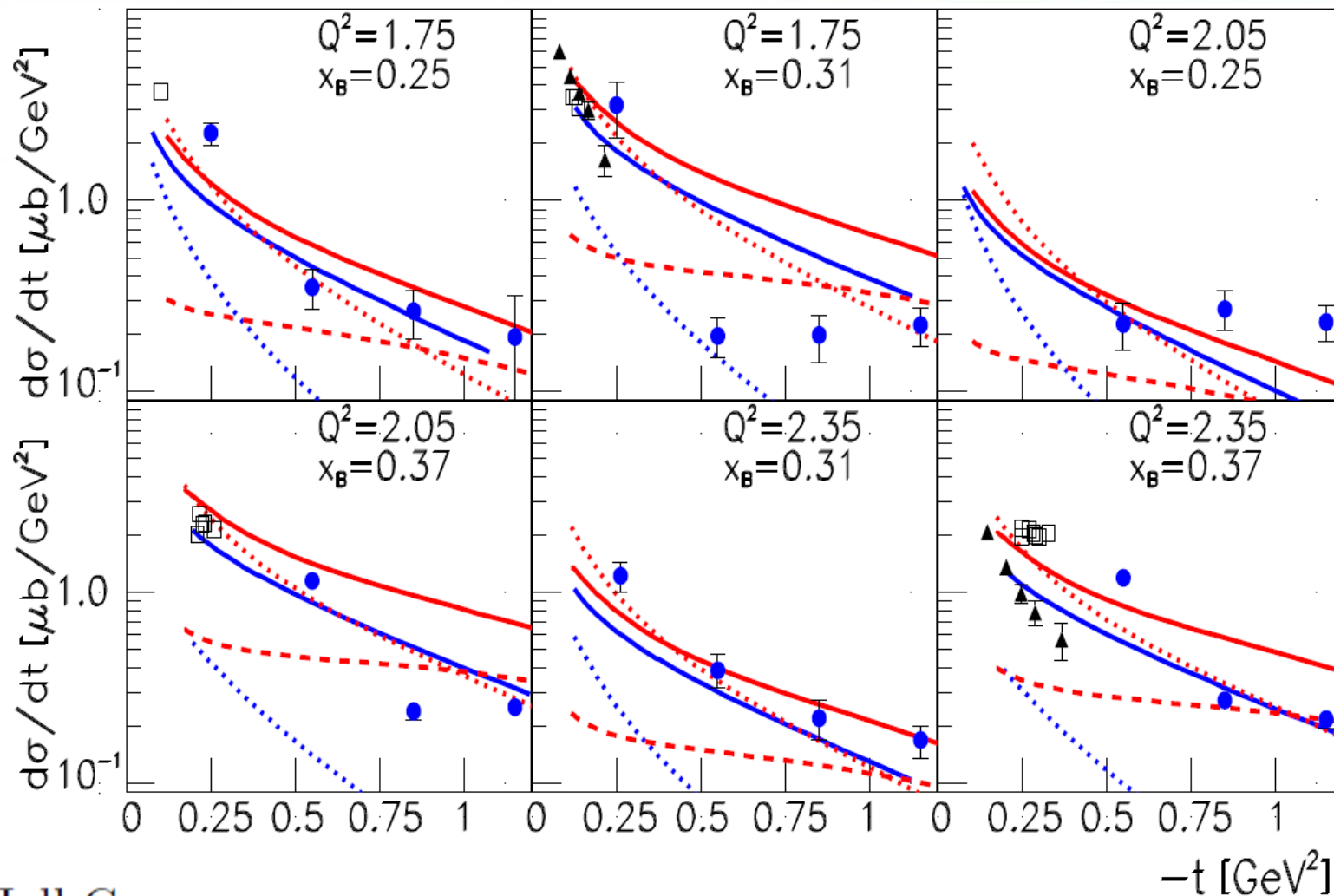
black open squares ( $d\sigma/dt$ )

X. Qian *et al.*, Phys. Rev. C 81, 055209 (2010).





# Cross-sections



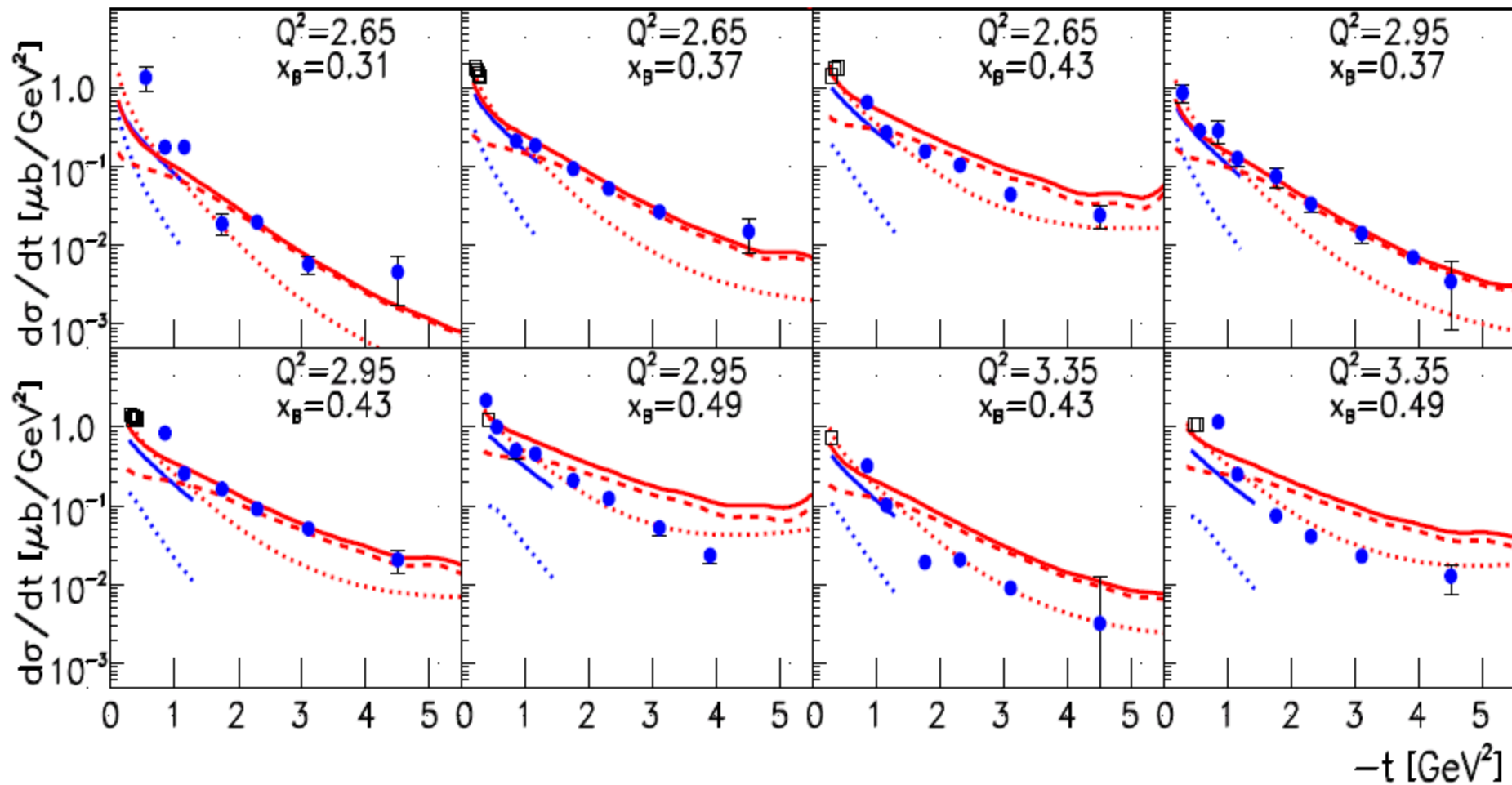
JLab Hall C

black solid triangles  $d\sigma_L/dt$

H. P. Blok *et al.*, Phys. Rev. C **78**, 045202 (2008).



# Cross-sections vs. $-t$





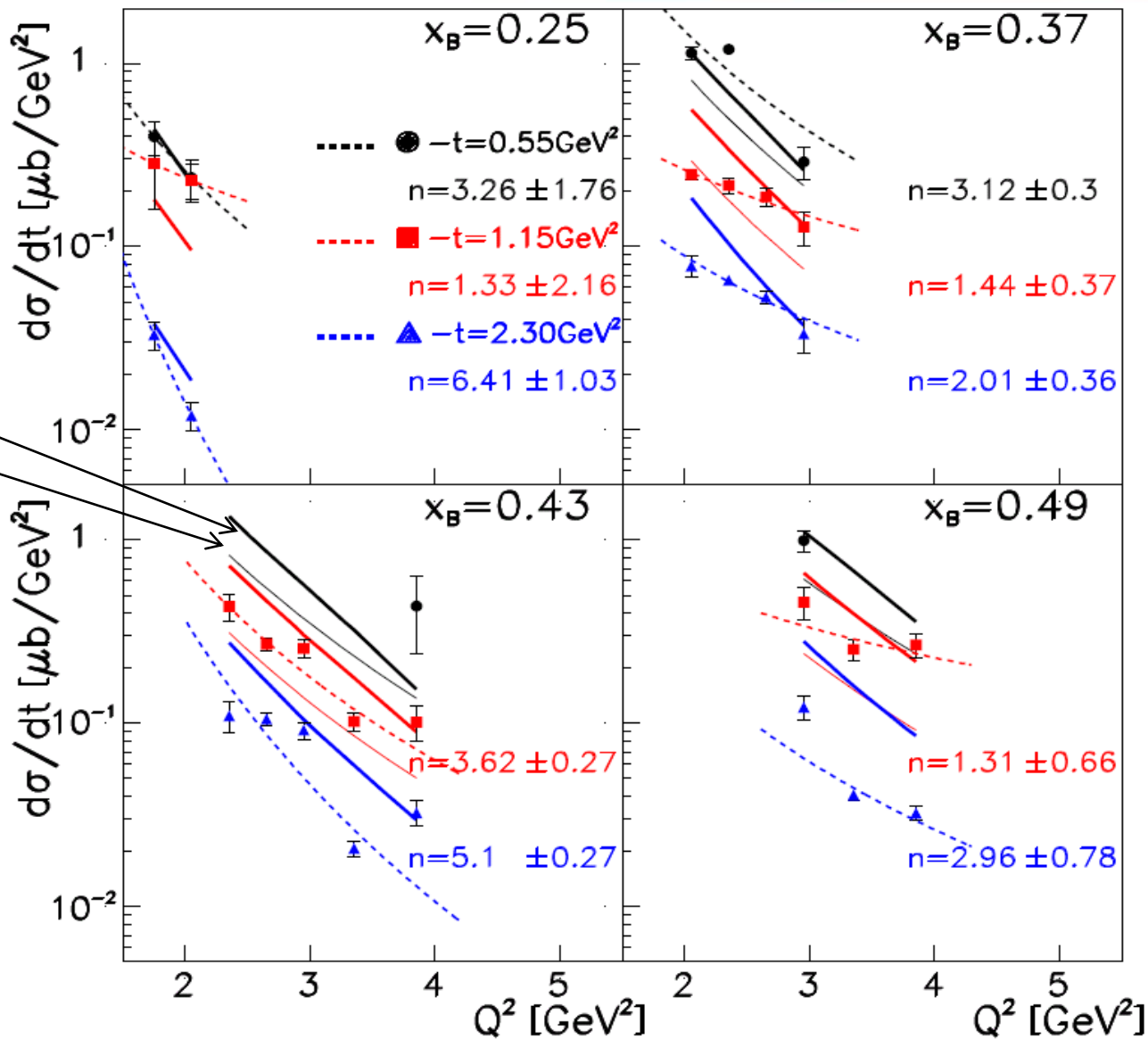


# Q<sup>2</sup> - scaling cross-sections

Fixed x, t

$$A/Q^n$$

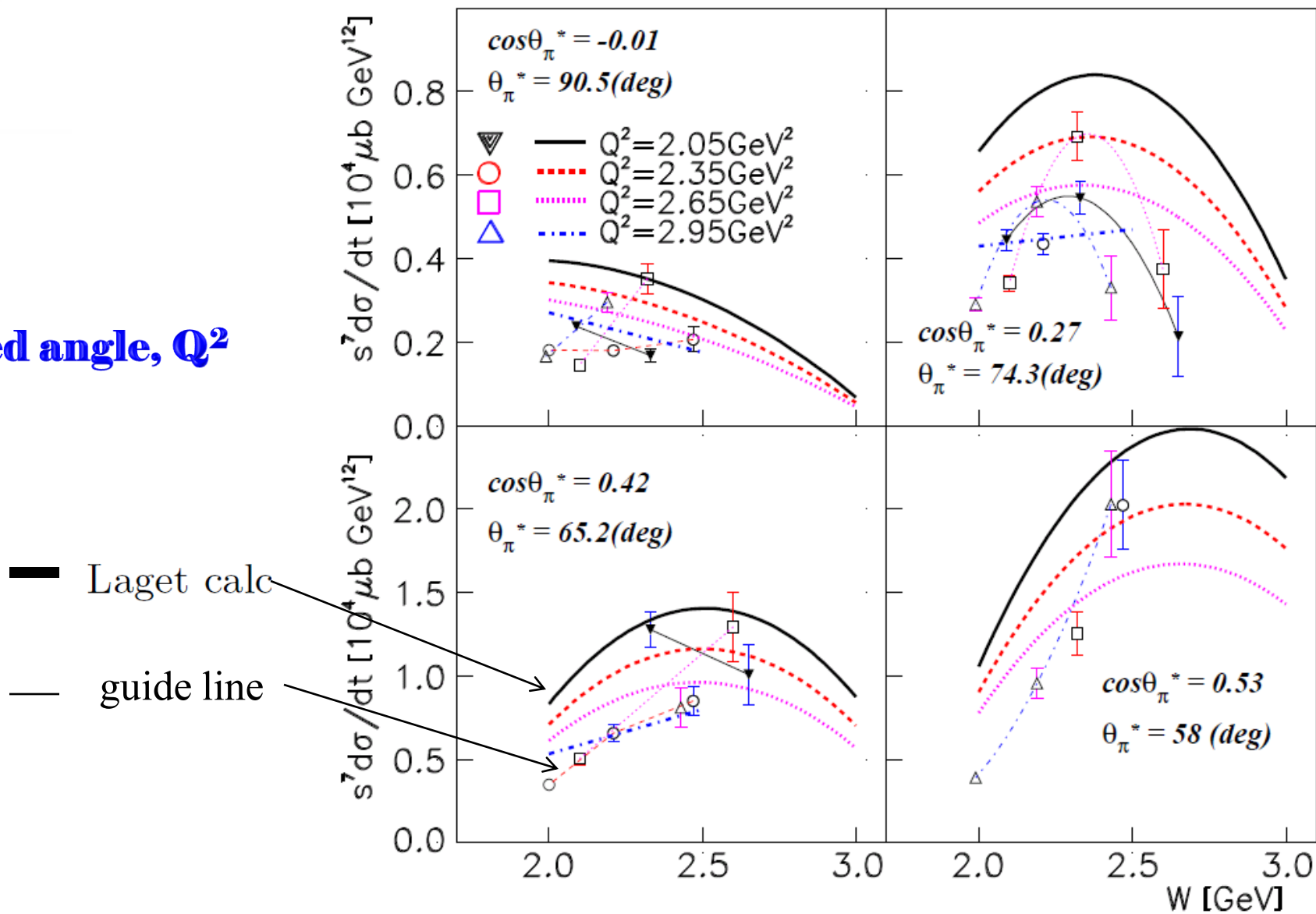
 Laget calc  
 GK calc





# S - scaled cross-sections

Fixed angle,  $Q^2$



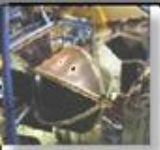


# Summary

- **We have measured the cross sections of  $p(e,e'\pi^+)n$  as a function of**
  - $-t = 0.1 - 5.3 \text{ GeV}^2$ ,  $x_B = 0.16 - 0.58$ ,  $Q^2 = 1.6 - 4.5 \text{ GeV}^2$ .**
- **Compared our differential cross sections to two recent calculations:**
  - ✓ **Hadronic degrees of freedom (Laget Regge)**
  - ✓ **Partonic degrees of freedom (GK handbag).**
- **Two approaches differ in the relative contributions of the longitudinal and transverse parts of the cross section, in particular as  $x_B$  increases**
- **If the handbag approach is confirmed, the  $p(e, e'\pi^+)n$  process offers the outstanding potential to access transversity -GPDs.**



**Thank you for your attention~!**



# Cross-sections vs. $-t$

**First time compare data with hadronic degree of freedom**

**Laget model : Reggeized  $\rho^+$  and  $\pi^+$  meson exchange in t-channel.**

**Laget model :**

- (1) Well-known (constraint) hadronic coupling constant**
- (2) Main free parameters = mass-scaled electromagnetic form factors @  $\gamma N$  vertex**
- (3) Use of the standard mono-pole form factor  $\rightarrow$  steeper t-slope than data**
- (4) Agreement with data is achieved by recovering mass scaled form factors and depending on  $|t|$ .**
- (5) The form factor is shrinking in size of the nucleon system as  $|t|$  increases.**  
**This size effect quantitatively same as  $\omega$ -electroproduction**
- (6) Laget calculation already gives a good description of the photo-production data (SLAC and JLab) and HERMES electro-production data.**  
**Note that this calculation has not been adjusted to fit our data.**
- (7) Calculation shows L-T crossing at  $-t \sim 1\text{GeV}^2$  overall kinematic regions.**
- (8) The dominance of  $\sigma_L$  at low  $|t|$  is a consequence of the t-channel  $\pi^+$ -exchange (pion pole)**  
**At large  $|t|$ ,  $\rho^+$  meson exchange which contributed by mostly to the transverse part of the cross-section begin to dominate.**
- (9) Laget model contains not only t-channel meson exchange but also u-channel baryon exchange. This can be shown in certain kinematic region such as large  $|t|$  and small  $|u|$ .**





# Cross-sections vs. -t

**GK model : handbag GPD formalism**

**$\sigma_L$  : mostly generated by the pion-pole (similar as Laget model)**

**\*\*\* Important difference : treatment of the pion-pole calculation**

**Laget model : t-channel propagator  $\propto s^{\alpha(t)}$**

**$\alpha(t)$  is the pion Regge trajectory**

**$Q^2$ , t-dependent electromagnetic form factor allows  
to have s-  $X_B^{\tau}$ , t- dependent of the pion-pole**

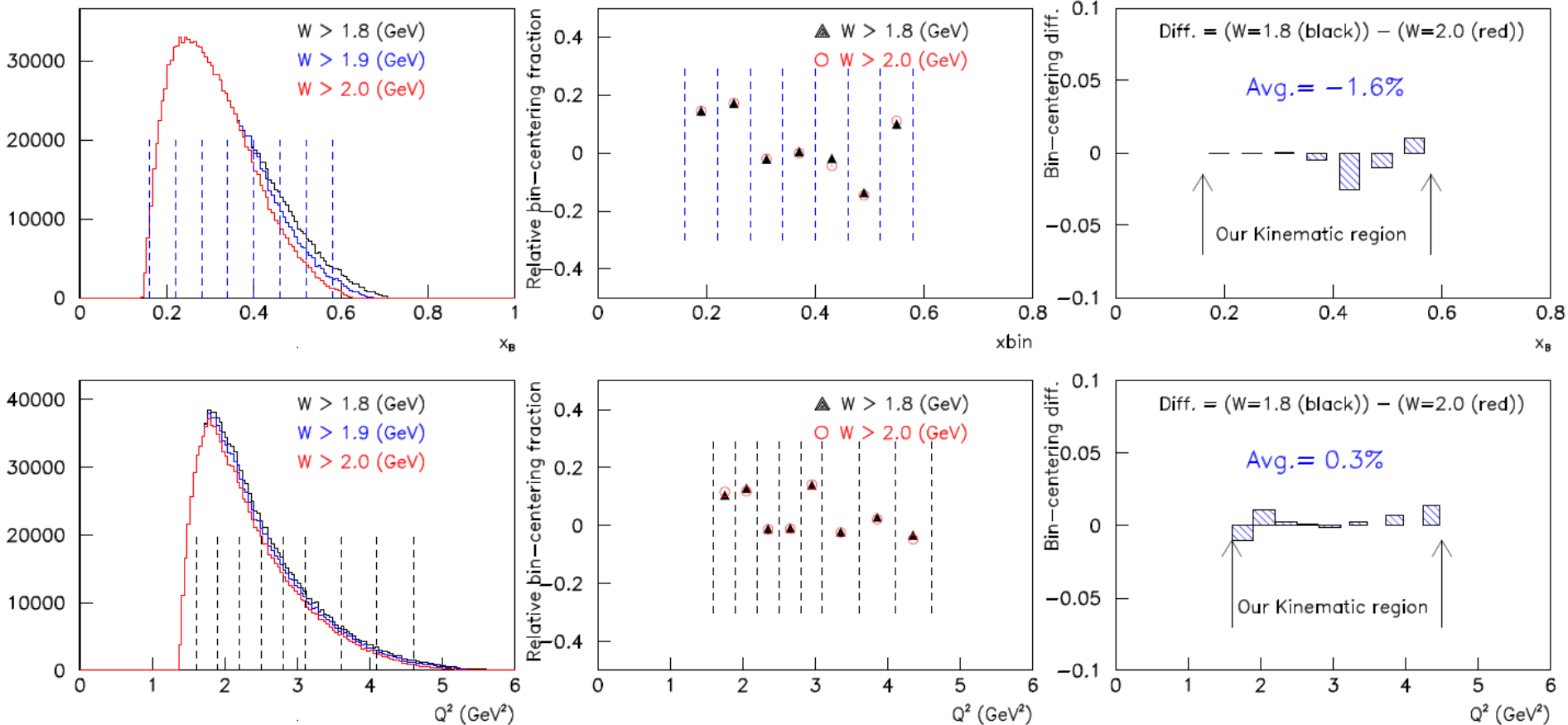
**GK model : t-channel pion propagator  $\propto 1/(t-m_{\pi}^2)$**

**no s-dependence.**

**The hadronic form factor at  $\pi NN$  vertex is only t-dependence.**

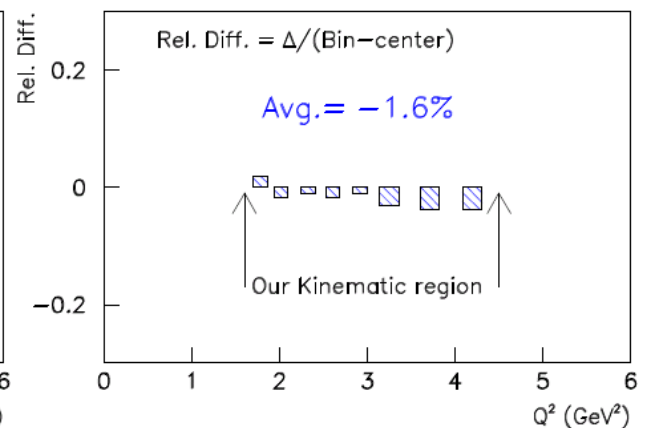
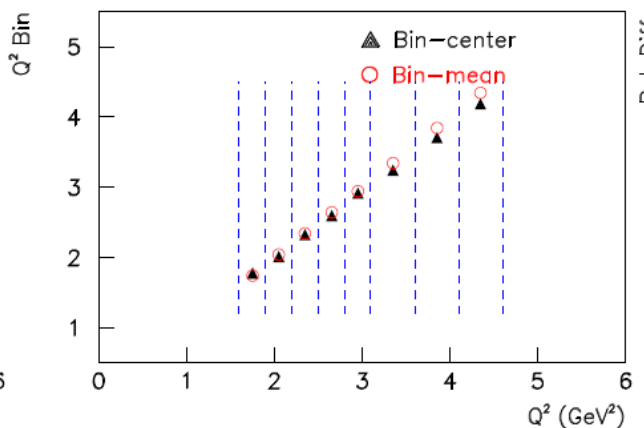
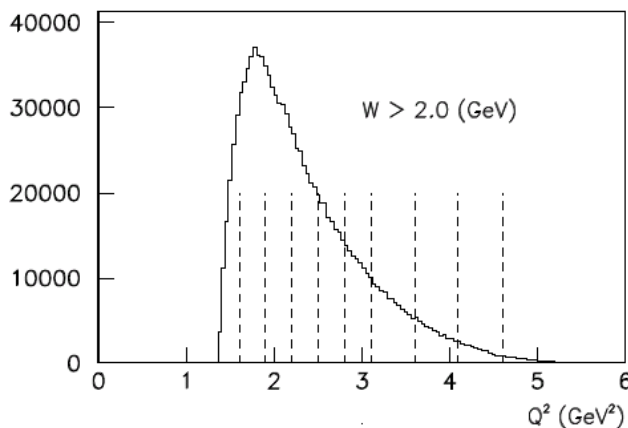
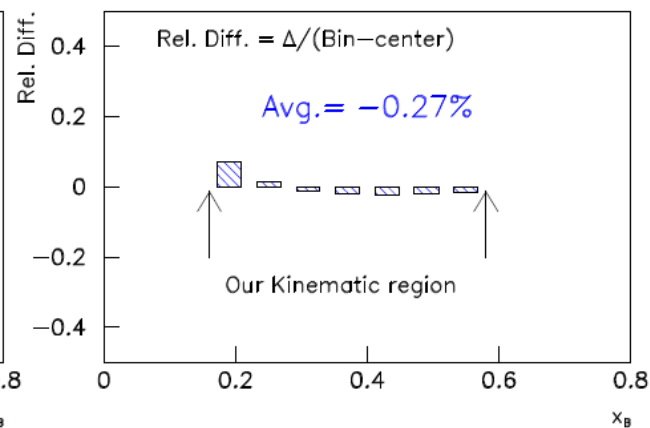
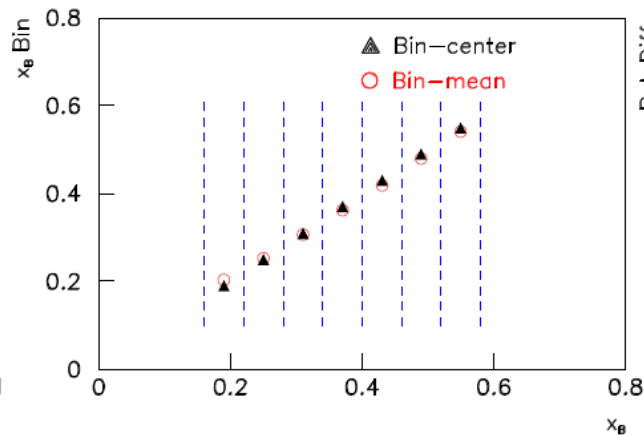
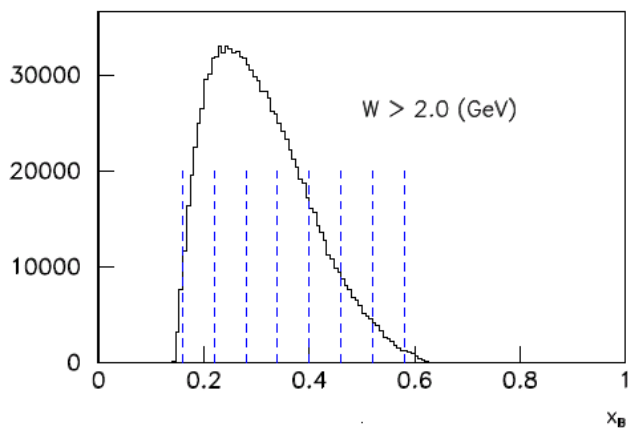


# Systematic uncertainties for bin-centering by $W$ cut



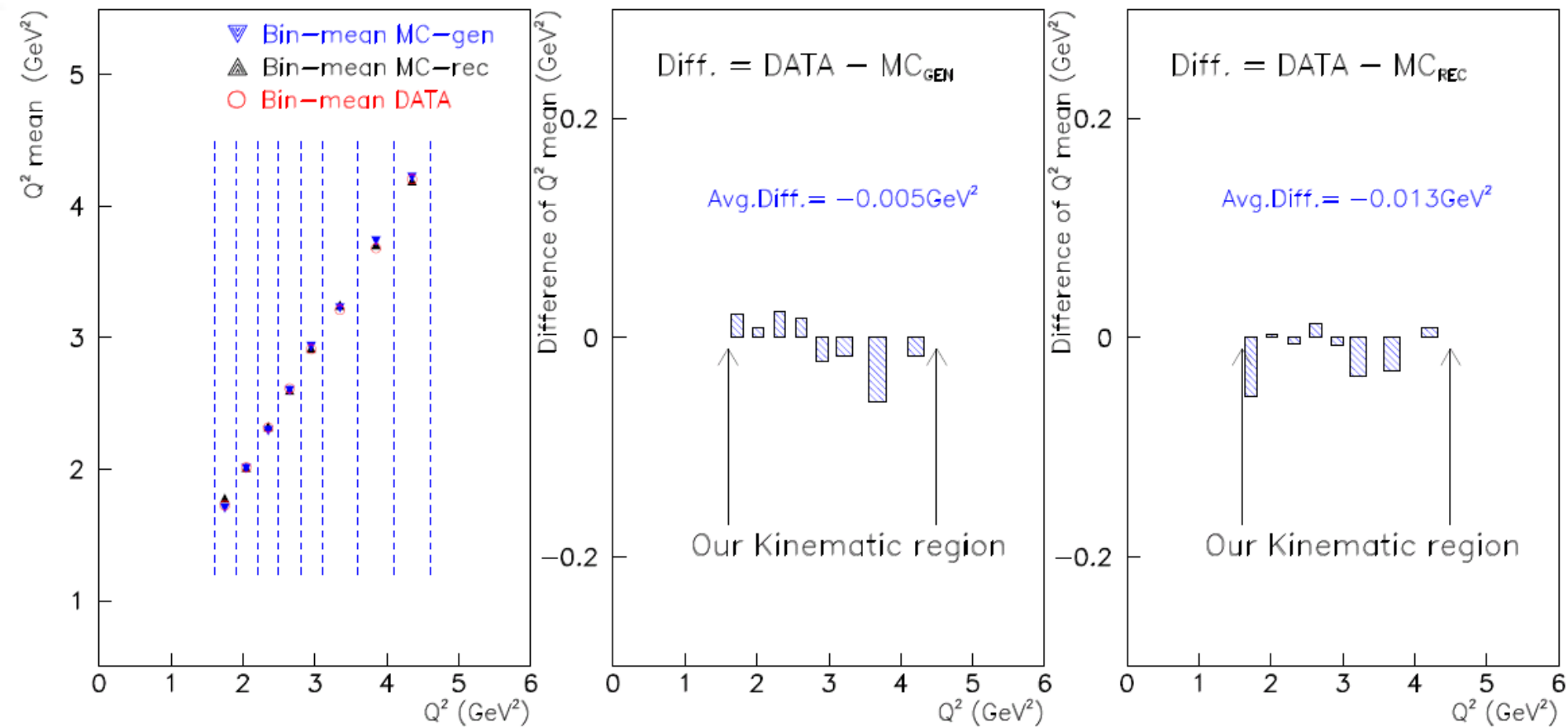


# Difference between bin-mean vs. bin-center



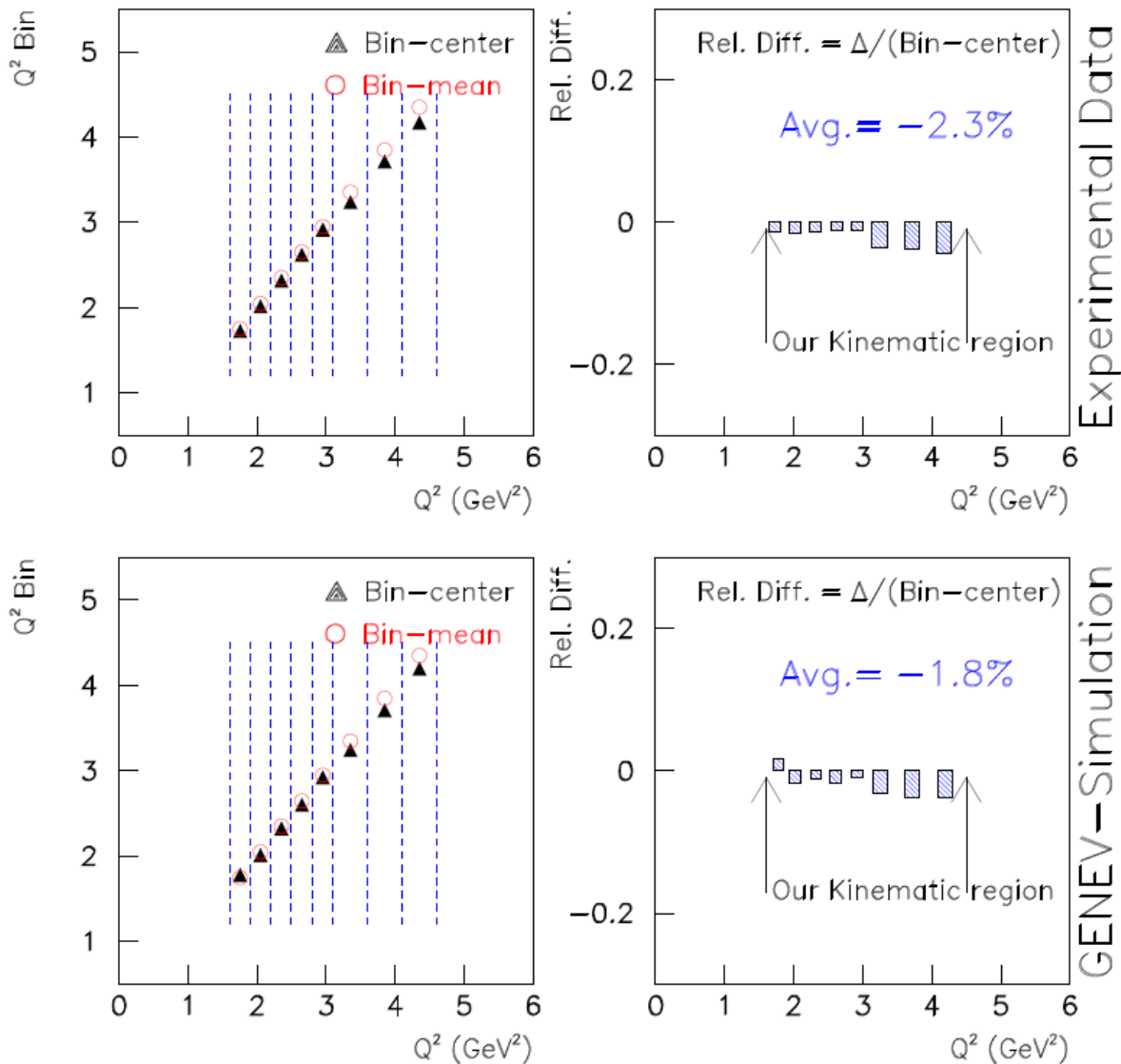


# Difference of bin-mean from GEN/REC/DATA





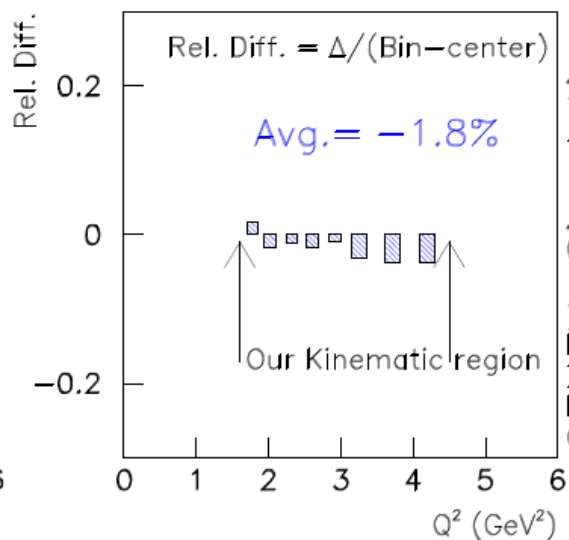
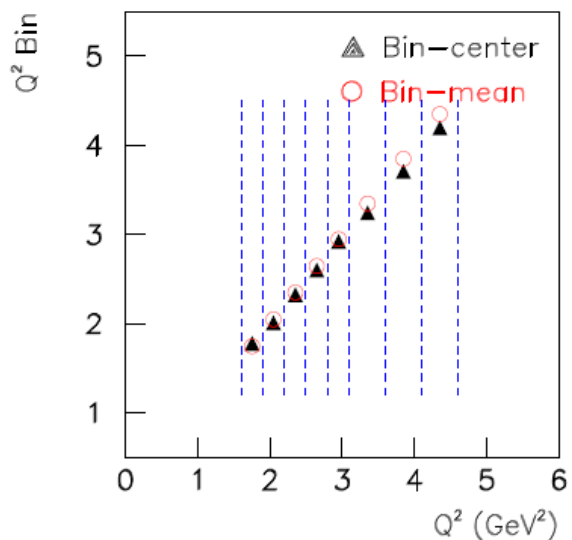
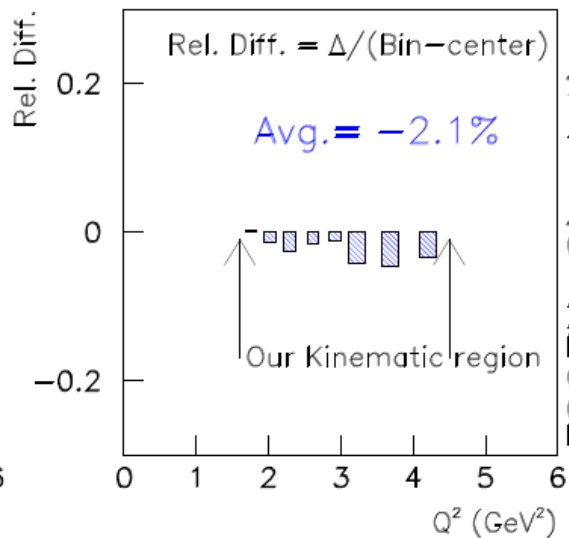
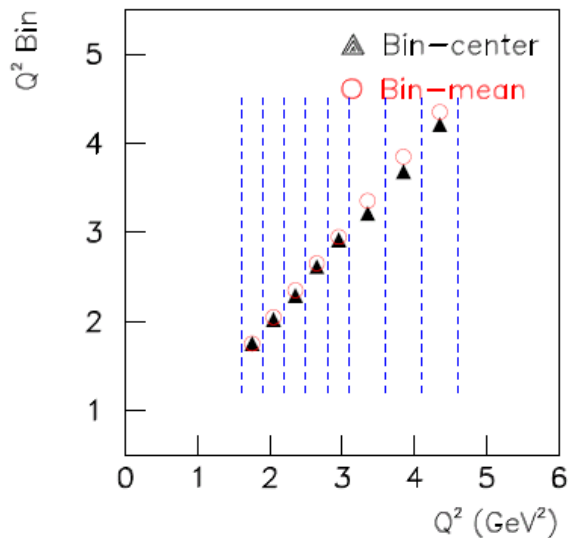
# Difference between bin-mean vs. bin-center





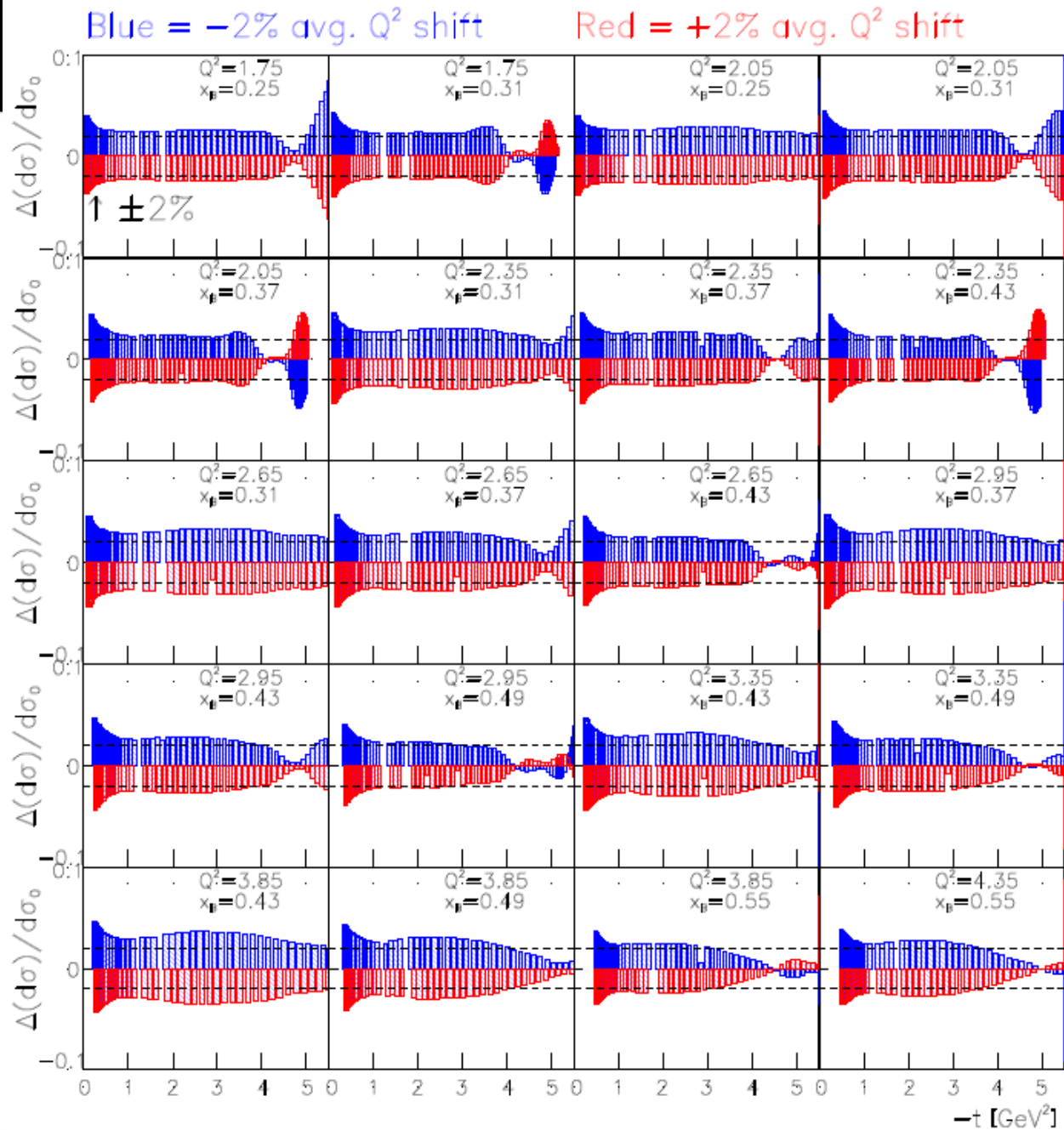


# Difference between bin-mean vs. bin-center





# Bin-effect by model

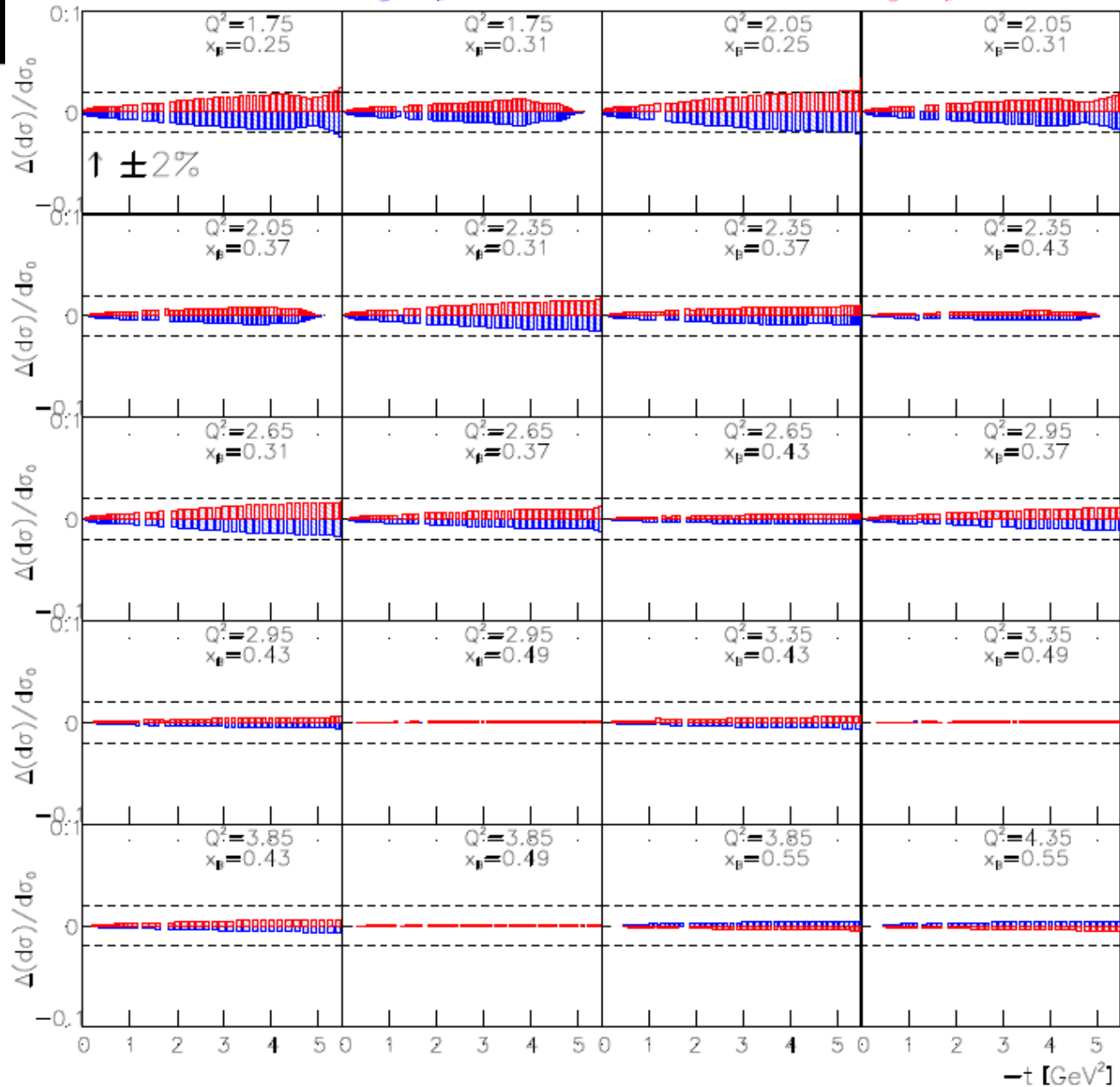




# Bin-effect by model

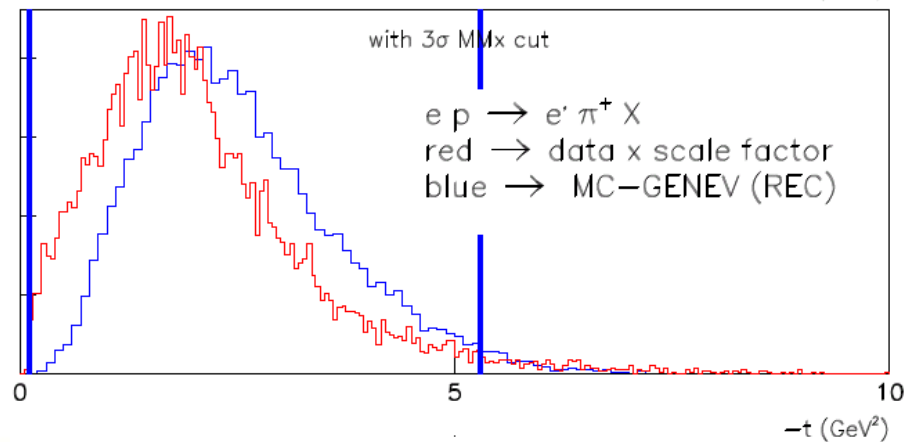
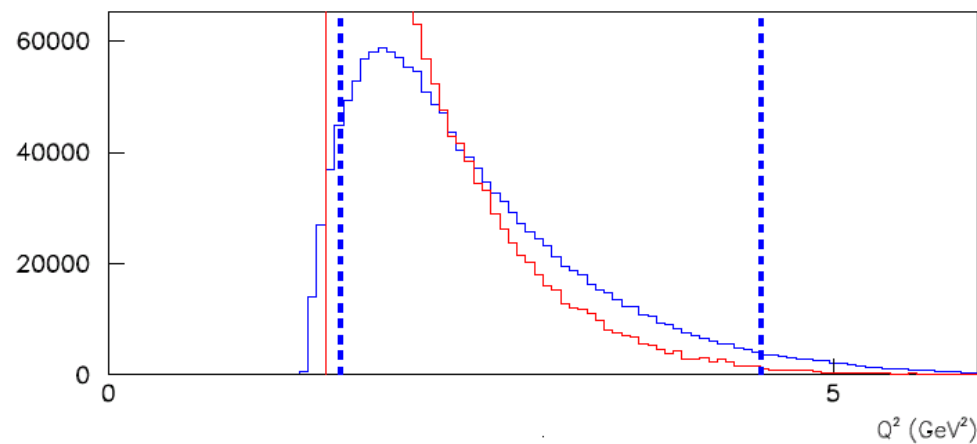
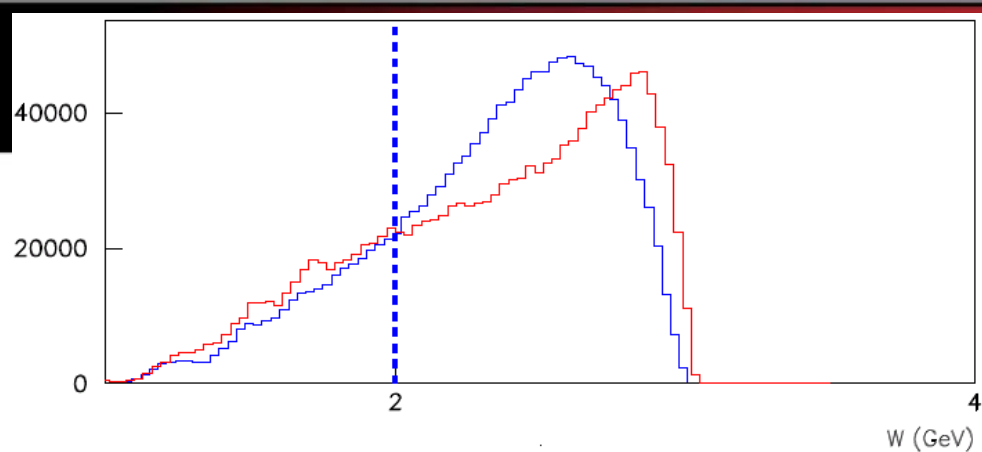
Blue =  $-0.3\%$  avg.  $x_B$  shift

Red =  $+0.3\%$  avg.  $x_B$  shift





# DATA vs. MC

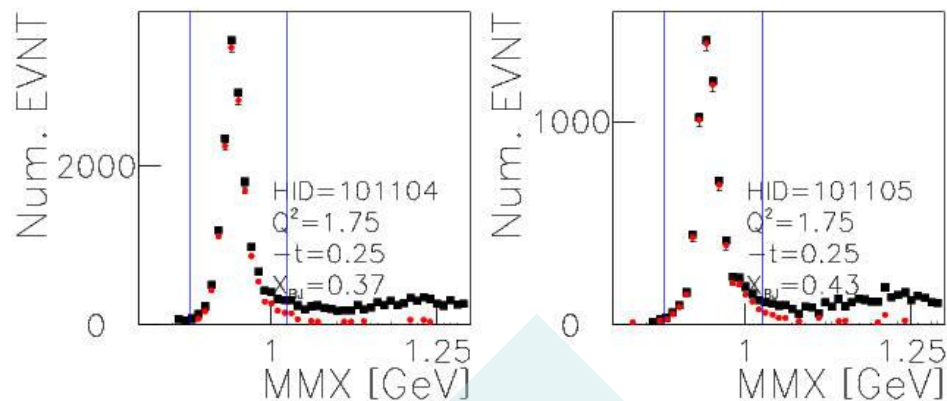
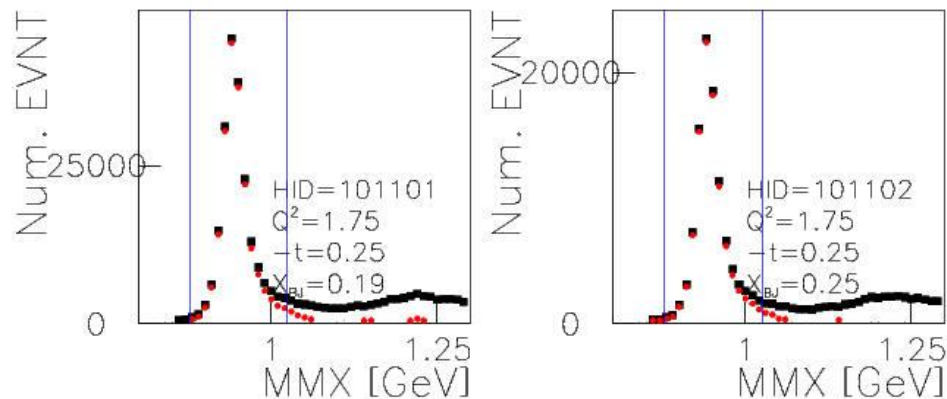




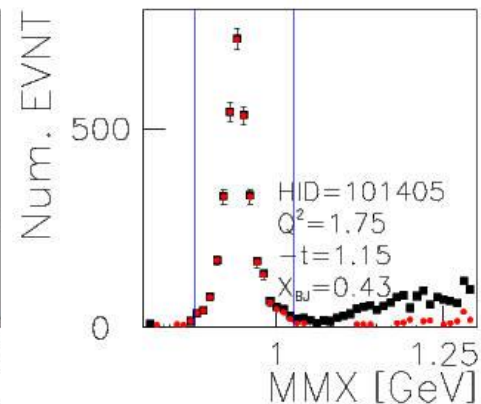
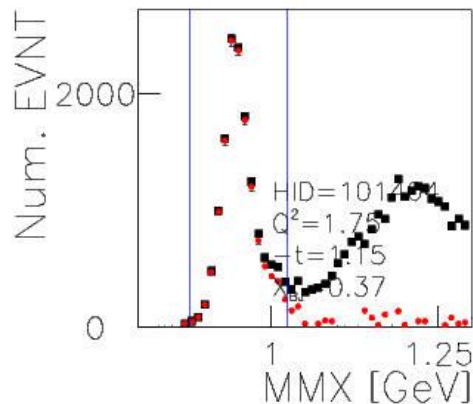
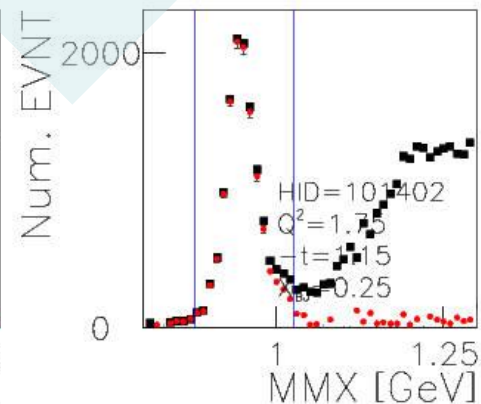
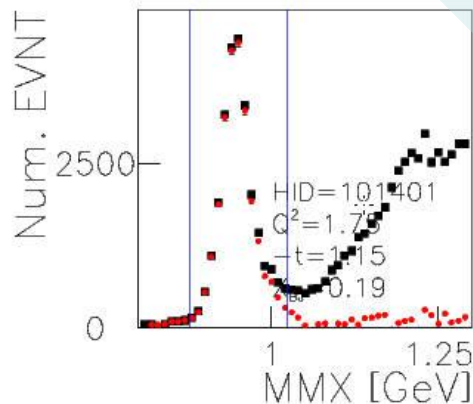
# Background subtraction

$Q^2 = 1.75 \text{ GeV}^2$

*High -t range*



*Low -t range*





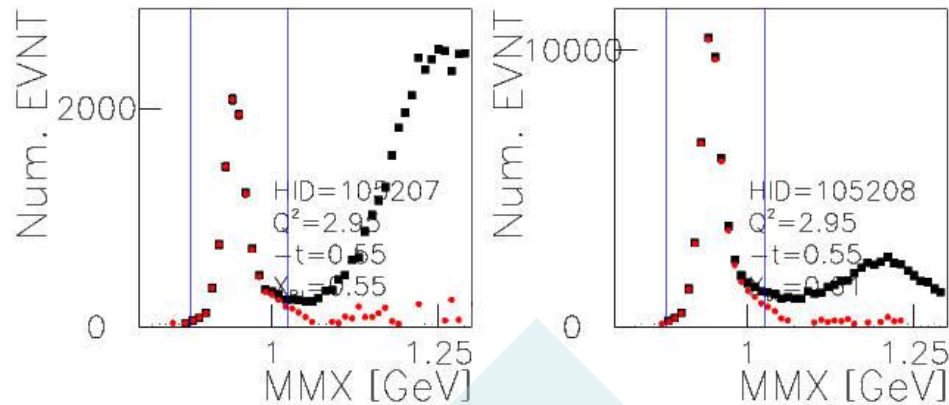
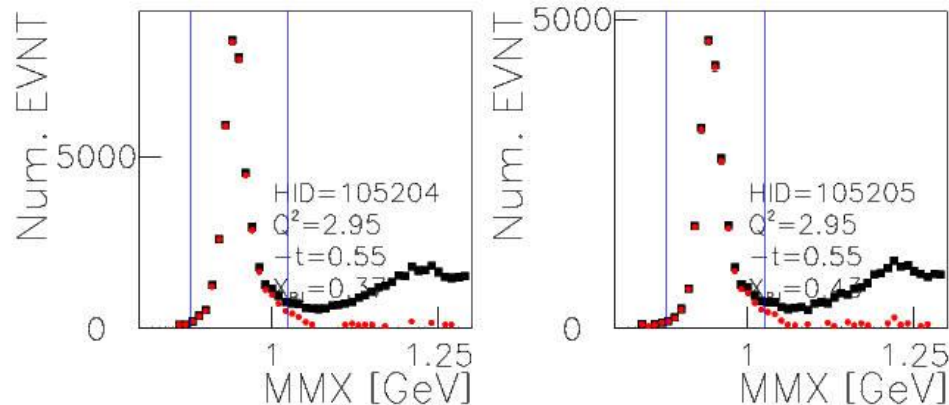


# Background subtraction

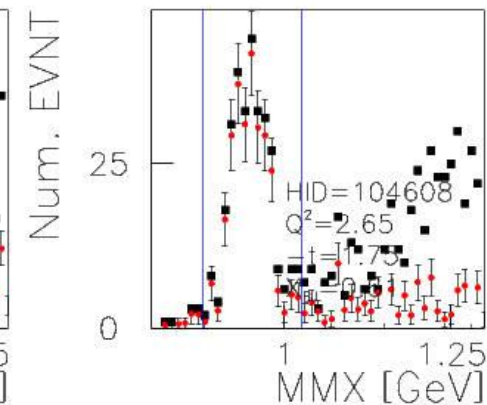
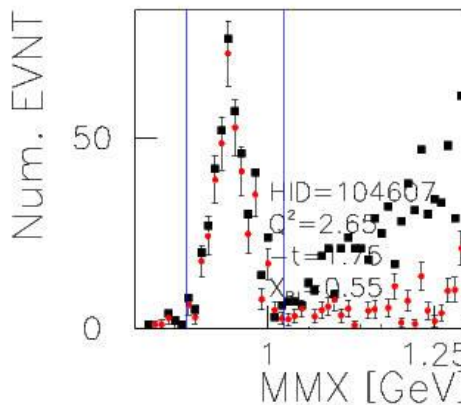
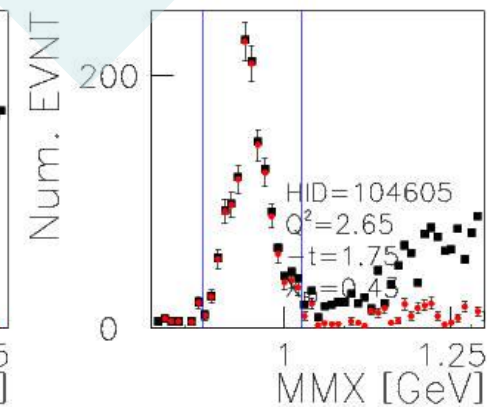
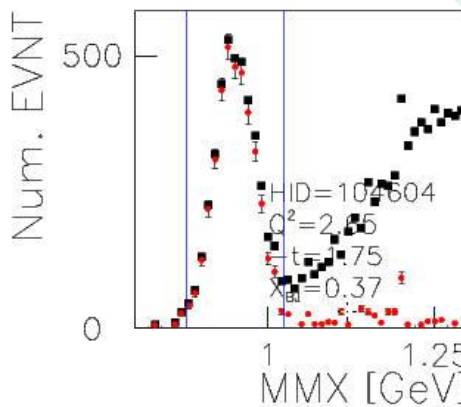
$Q^2 = 2.65 \text{ GeV}^2$

$Q^2 = 2.95 \text{ GeV}^2$

*High -t range*

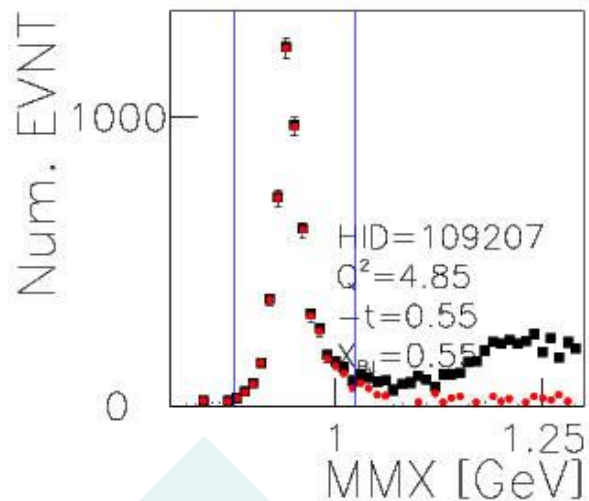


*Low -t range*

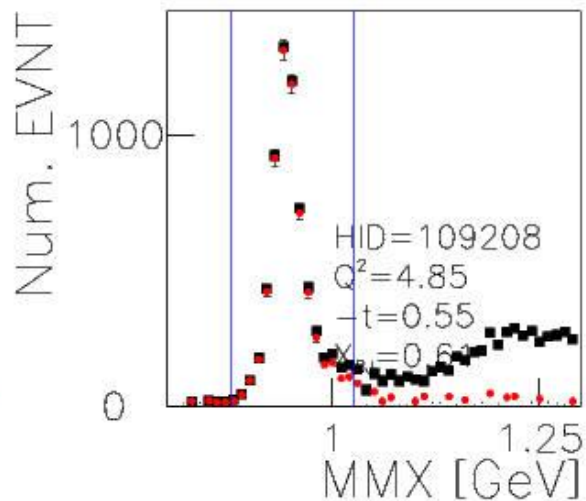




# Background subtraction

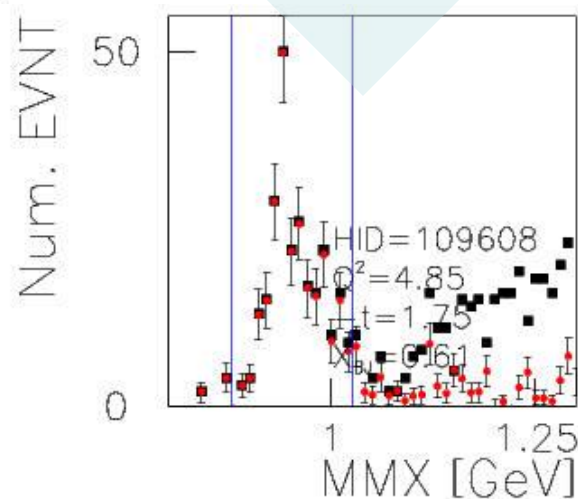
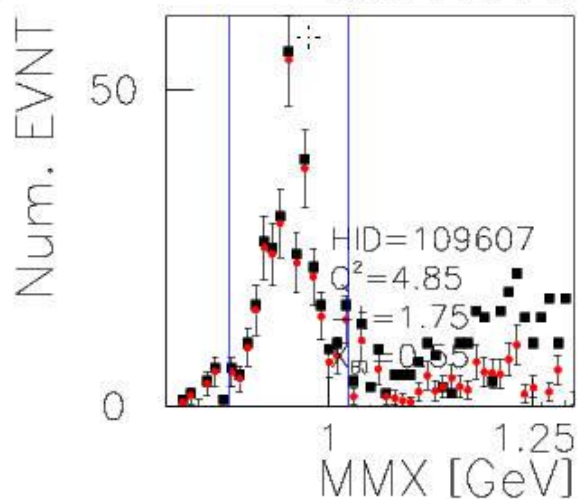


*Low -t range*



$Q^2 = 4.85 \text{ GeV}^2$

*High -t range*

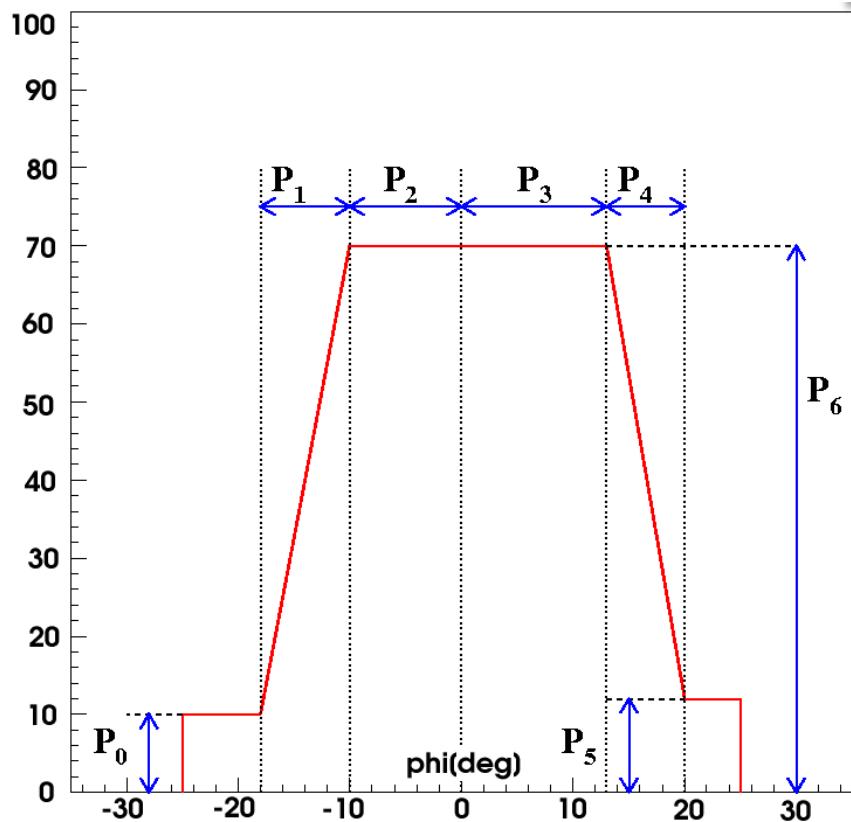




# Analysis - fiducial cuts

## FID( $\pi^+$ )

$$f = \begin{cases} P_0 & : \phi < P_2 - P_1 \\ \frac{P_6 - P_0}{P_1}(\phi - P_2 + P_1) + P_0 & : P_2 - P_1 \leq \phi < P_2 \\ P_6 & : P_2 \leq \phi < P_3 \\ \frac{P_6 - P_5}{P_4}(-\phi + P_3 + P_4) + P_5 & : P_3 \leq \phi < P_3 + P_4 \\ P_5 & : P_3 + P_4 \leq \phi \end{cases}$$



402.SLIY.12

