Homework Set 8

University of South Carolina

Instructor: Ralf W. Gothe

## 8.1) Callan-Gross Relation

8.1.1) [4] Derive the Callan-Gross relation that connects the structure functions $F_{1}$ and $F_{2}$ !

## 8.2) Deep Inelastic Scattering

Deep inelastic electron-proton scattering is studied at the HERA collider. Electrons with 30 GeV are collided head on with 820 GeV protons.
8.2.1) [3] Calculate the center of mass energy of this reaction. What energy does an electron beam, that hits a stationary proton target, have to have to reproduce this center of mass energy?
8.2.2) [4] The relevant kinematic quantities in deep inelastic scattering are the square of the four momentum transfer $Q^{2}$ and the Bjorken scaling variable $x$. You already have derived $Q^{2}$ in dependence of the electron's kinematic variables $E_{e}$, the beam energy, $E_{e}^{\prime}$, the energy of the scattered electron and $\vartheta_{e}$, the electron scattering angle. In certain kinematic regions it is better to extract $Q^{2}$ from other variables since their experimental values give $Q^{2}$ with smaller errors. Find a formula for $Q^{2}$ that depends only on the scattering angles of the electron $\vartheta_{e}$ and of the scattered quark $\gamma_{q}$ as well as $E_{e}$. How may $\gamma_{q}$ be determined experimentally from the measured hadron energies and momenta of the final state?
8.2.3) [2] Show that the four momentum transfer $Q^{2}$ at HERA equals in good approximation $s$, if you consider an electron scattering angle $\vartheta_{e}$ of $180^{\circ}$ ! Use $s^{2}$ and $Q^{4}$.
8.2.4) [2] What is the largest possible four momentum transfer $Q^{2}$ at HERA? What $Q^{2}$ values are attainable in experiments with stationary targets and 30 GeV electron beam energies? Estimate and compare the spatial resolutions within the proton in both cases!
8.2.5) [GS] [2] Find the kinematic region in $Q^{2}$ and $x$ that can be reached with the ZEUS calorimeter, which covers the angular region $7^{\circ}$ to $178^{\circ}$. The scattered electron needs to have at least 5 GeV to be resolved.

