

Homework Set 6

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3/13/24

6.1) **Diffractive Scattering**

Fraunhofer diffraction by a circular disk of a diameter D produces pattern of concentric diffraction rings. The first minimum appears at $\vartheta = 1.22 \frac{\lambda}{D}$.

- 6.1.1) [5] Determine the angular separation of the diffraction minima in α scattering off a ^{56}Fe nucleus for a given kinetic energy of the α particles in the lab frame $E_\alpha = 100 \text{ MeV}$. Both nuclei should be considered as impenetrable disks. Calculate first the CMS momentum p_α^* of the α particle, then the corresponding de-Broglie wave length $\lambda^* = \frac{h}{p_\alpha^*}$ and then the scattering angle ϑ^* .
- 6.1.2) [5] Determine the scattering angle ϑ in the lab frame. Calculate first the CMS momentum p_α^* , then the velocity of the CMS with respect to the lab frame $\beta = \frac{p_\Sigma}{E_\Sigma}$, then the momentum p'_α in the lab frame and finally the scattering angle ϑ in the lab frame!

6.2) **Electron Radius**

- 6.2.1) [5] Suppose one wants to obtain an upper bound for the electron radius by looking for a deviation from the Mott cross section in electron electron scattering and that this cross section can be measured with an uncertainty of 1%. What center of mass energy is necessary to set the upper limit for the electron radius to 10^{-18} m ?
- 6.2.2) [3] Calculate the needed primary electron energy (*ies*) for a fixed target (*collider*) experiment!
- 6.2.3) [2] What would be the necessary center of mass energy, if the cross section is measured to a precision of 0.01%?